



Searches for Neutrinos in the Direction of Radio-bright Blazars with the ANTARES Telescope

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Abstract

Active galaxies, especially blazars, are among the most promising extragalactic candidates for high-energy neutrino sources. To date, ANTARES searches included these objects and used GeV–TeV γ -ray flux to select blazars. Here, a statistically complete blazar sample selected by their bright radio emission is used as the target for searches of origins of neutrinos collected by the ANTARES neutrino telescope over 13 yr of operation. The hypothesis of a neutrino–blazar directional correlation is tested by pair counting and a complementary likelihood-based approach. The resulting posttrial p -value is 3.0% (2.2σ in the two-sided convention). Additionally, a time-dependent analysis is performed to search for temporal clustering of neutrino candidates as a means of detecting neutrino flares in blazars. None of the investigated sources alone reaches a significant flare detection level. However, the presence of 18 sources with a pretrial significance above 3σ indicates a $p = 1.4\%$ (2.5σ in the two-sided convention) detection of a time-variable neutrino flux. An a posteriori investigation reveals an intriguing temporal coincidence of neutrino, radio, and γ -ray flares of the J0242+1101 blazar at a $p = 0.5\%$ (2.9σ in the two-sided convention) level. Altogether, the results presented here suggest a possible connection of neutrino candidates detected by the ANTARES telescope with radio-bright blazars.

Unified Astronomy Thesaurus concepts: [Neutrino astronomy \(1100\)](#); [Blazars \(164\)](#)

1. Introduction

Astrophysical neutrinos of high energies, TeV and above, were discovered almost 10 yr ago by the IceCube Collaboration (Aartsen et al. 2014), consistent with later studies with the other two existing instruments, namely, ANTARES (Fusco & Versari 2019) and Baikal-GVD (Allakhverdyan et al. 2023). However, their origins are still not fully determined. Observational evidence exists for a wide range of neutrino sources, including individual active galaxies (Aartsen et al. 2018a, 2018b; Abbasi et al. 2022a), large samples of blazars (Giommi et al. 2020; Plavin et al. 2020, 2021, 2023; Buson et al. 2022, 2023; Kun et al. 2022; Abbasi et al. 2023a), and the Milky Way (Albert et al. 2017a, 2018a, 2023; Neronov & Semikoz 2016; Aartsen et al. 2019; Kovalev et al. 2022; Abbasi et al. 2023b).

Active galaxies, particularly blazars that have their jets pointed toward us, formed a very promising class of high-energy neutrino sources even before direct observational evidence became available Berezinsky (1977), Eichler (1979), Murase (2017), Boettcher (2019). The emission from the jet is

detectable across cosmological distances thanks to the relativistic beaming Blandford et al. (2019). Similar beaming effects should influence neutrinos as well, enhancing their chance to be detected on Earth (Boettcher 2023; Plavin et al. 2023). Neutrino production itself is not affected by the direction of the jet, and similar nonbeamed active galaxies can be expected to emit comparable neutrino fluxes. They are likely only detectable at closer distances, though. Moreover, there are observational hints of neutrinos being predominantly produced during major flares close to the jet origin Plavin et al. (2020), Hovatta et al. (2021), indicating a tight physical connection between relativistic jets and neutrino production processes.

Currently, all associations of high-energy neutrinos with celestial objects or classes thereof are fundamentally statistical. The comparison of findings based on different instruments is crucial to understand both astrophysical neutrino flux characteristics, such as its energy spectrum, and potential systematic effects inherent to their detection. Earlier searches for a neutrino signal in the ANTARES detector from the direction of blazars were performed using γ -bright blazars contained in the Fermi LAT catalog Adrian-Martinez et al. (2015); Albert et al. (2021a). However, recent studies suggest that emission and flares in γ -rays may not be tightly correlated with neutrino sources Abbasi et al. (2021), Plavin et al. (2021), Boettcher et al. (2022); hadronic γ -rays are coproduced together with neutrinos but quickly cascade down in energy. Synchrotron emission from blazar jets, detected on Earth as

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radio emission, could likely be a better tracer of relativistic beaming and activity happening close to the jet origin.

In addition, the recent publication of the IceCube Event Catalog of Alert Tracks-1 Abbasi et al. (2023c), containing a revised sample of neutrino candidates with a high probability of being of astrophysical origin, has been followed by a search Abbasi et al. (2023d) for a correlation with the population of blazars contained in the Fermi 4LAC-DR2 catalog and the Radio Fundamental Catalog. As no significant correlation is found, this result mitigates the previous findings of Plavin et al. (2020) and indicates that only a minority of the γ -ray-bright and radio-bright AGN population can be identified as potential sources of high-energy neutrinos.

This paper presents an independent and complementary study of the possible neutrino–blazar association with data collected by the ANTARES observatory. Section 2 and Section 3 define the data set used in the analysis: the ANTARES neutrino candidates and the radio observations of inner blazar regions. A description of the employed analysis methods and respective results follows. The hypothesis of directional correlation between neutrinos and blazar emission is tested by mean of a neutrino–blazar pair-counting method (Section 4), as well as a complementary time-integrated likelihood-based approach (Section 5). Moreover, in order to search for a time clustering of ANTARES events coming from the blazar directions, a time-dependent likelihood scan is also performed (Section 6). In Section 7, the results of a follow-up search for multimessenger time flare associations are presented. Finally, Section 8 summarizes all findings and discusses further prospects.

2. ANTARES Detector and Data Sample

ANTARES Ageron et al. (2011) was an undersea high-energy neutrino telescope located 40 km offshore from Toulon, France, below the surface of the Mediterranean Sea. After over 15 yr of operation, it took its last data in 2022 February. The detector consisted of a three-dimensional array of 885 photomultiplier tubes (PMTs) distributed along 12 vertical lines of 450 m length, for a total instrumented volume of $\sim 0.01 \text{ km}^3$. Each line was anchored to the seabed at a depth of about 2500 m and held taut by a buoy at the top. The PMTs inside pressure-resistant optical modules Amram et al. (2002) collected the Cherenkov photons induced by the passage of the relativistic charged particles produced in neutrino interactions inside or near the instrumented volume. The information provided by the position, time, and collected charge in the PMTs corresponds to a hit Aguilar et al. (2007). Hits are used to infer the direction and energy of the incident neutrino.

Two main event topologies, induced by different neutrino flavors and types of interactions, could be identified: tracklike and shower-like events Albert et al. (2021b). Charged current (CC) interactions of muon neutrinos produce relativistic muons that can travel large distances through the medium, with Cherenkov light being induced all along the muon path, resulting in a tracklike signature in the detector Aguilar et al. (2011), Adrian-Martinez et al. (2013). The parent neutrino direction of high-quality selected tracks can be reconstructed with a median angular resolution of $\sim 0.8^\circ$ at $E_\nu \sim 1 \text{ TeV}$ and below $\sim 0.4^\circ$ for $E_\nu > 10 \text{ TeV}$ Albert et al. (2017b) thanks to the long lever arm of this channel. Shower-like events are induced by all-flavor neutral current as well as ν_e and ν_τ CC interactions Albert et al. (2017c). This topology is

characterized by an almost spherical light emission around the shower maximum with an elongation of a few meters, which results in a worse estimation of the parent neutrino direction compared to the track channel. A median angular resolution of $\sim 3^\circ$ is achieved for high-quality selected showers with energies between 1 TeV and 0.5 PeV Albert et al. (2017b).

The data set employed in this analysis includes events recorded in ANTARES between 2007 January 29 and 2020 February 29 (3845 days of live time) and selected using the criteria defined in Albert et al. (2017b), optimized to minimize the neutrino flux needed for a 5σ discovery of a pointlike source with a $\propto E^{-2.0}$ emission spectrum. The selection includes cuts on the zenith angle, the angular error estimate, and parameters describing the quality of the reconstruction. In the shower channel, an additional cut is applied on the interaction vertex, required to be located within a fiducial volume slightly larger than the instrumented volume. Recently improved calibrations have been used to reconstruct all the selected ANTARES events. This yields slightly different values of the reconstructed direction—with $\sim 98\%$ of the selected events being reconstructed within 1° from the previous direction—and the quality parameters associated with each event. In addition, the energy estimator for tracklike events has been refined to take into account the time evolution of the detector Albert et al. (2018b) over the whole data-taking period. A total of 10,504 tracklike and 227 shower-like events survive the selection, with an expected atmospheric muon contamination of $\sim 14\%$ and $\sim 43\%$ for the track and the shower channel, respectively. Only the track channel is employed in the search for directional correlations, while the search for neutrino temporal flares makes use of both tracks and showers.

3. Radio Observations of Blazars

Synchrotron emission from inner regions of blazar jets is observed and measured by radio telescopes using very long baseline interferometry (VLBI) techniques. VLBI-measured flux densities represent the emission from the very central parsecs of blazars, and these measurements are used to select the objects included in this analysis.

A complete flux-limited sample of blazars observed by VLBI is selected using the same criteria as in Plavin et al. (2021). Accurate positions and parsec-scale flux densities of observed blazars are compiled in the Radio Fundamental Catalog.⁵⁸ Observations at 8 GHz are utilized because of their completeness across the whole sky. There are 3411 blazars with a historical average flux density above 150 mJy; 3051 of them fall into the ANTARES field of view and are targeted by the searches for directional correlations. Figure 1 shows the location of the selected blazars in equatorial coordinates, together with the ANTARES neutrino candidates. As for the time-dependent scan, the sources with low visibility, i.e., located above 40° in decl., are excluded from the search, leading to a targeted catalog of 2774 blazars. The collection of observations includes geodetic VLBI (Petrov et al. 2009; Piner et al. 2012; Pushkarev & Kovalev 2012), the Very Long Baseline Array (VLBA) calibrator surveys (Beasley et al. 2002; Fomalont et al. 2003; Petrov et al. 2005, 2006, 2008; Kovalev et al. 2007; Gordon et al. 2016; Petrov 2021), other 8 GHz global VLBI, VLBA, European VLBI Network, and Australian

⁵⁸ http://astrogeo.smce.nasa.gov/sol/rfc/rfc_2020d/

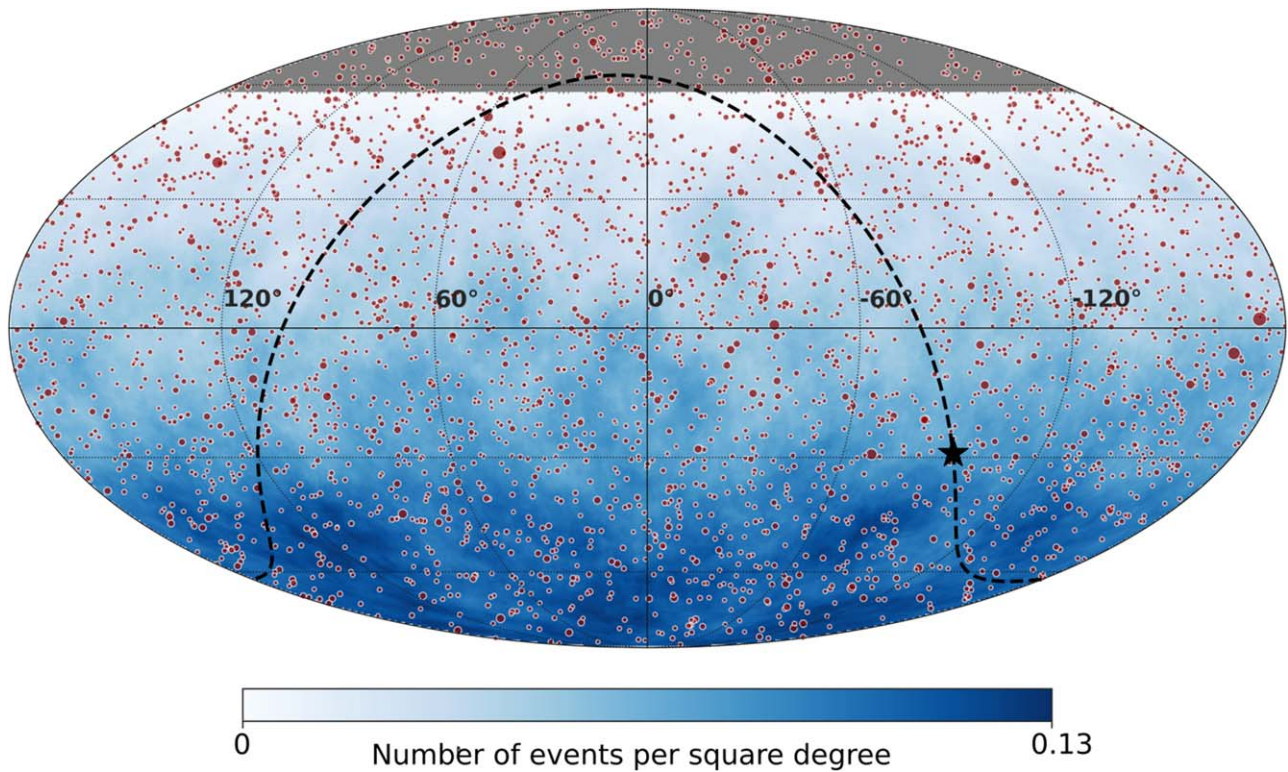


Figure 1. Equatorial sky map showing the location of the VLBI blazars (red dots), together with the average density of ANTARES tracklike and shower-like events per square degree. The event density at a given point in the sky is obtained by dividing the number of events found within a cone of 10° radius around this point by the solid angle of the cone. The surface of the markers is proportional to the VLBI 8 GHz flux density. The blazars located in the gray region at high declinations are outside the ANTARES field of view. The dashed black line shows the Galactic plane, and the Galactic center is represented by a black star.

Long Baseline Array programs (Petrov et al. 2011a, 2011b, 2019; Petrov 2011, 2012, 2013; Schinzel et al. 2015; Shu et al. 2017).

4. Counting Method

The first correlation analysis uses a simple method, inspired by Plavin et al. (2020), where the observable is the number of neutrino–blazar angular pairs separated by an angular distance Ψ less than $x \cdot \beta$. Here, β is the angular uncertainty coming from the neutrino reconstruction, and x is a free parameter that varies in the interval $[0.1; 2.0]$. The parameter x is meant to take into account a possible systematic difference between the output of the reconstruction algorithm and the true (unknown) angular error radius. Using Monte Carlo simulations, the relationship between the error estimate β and the true 68% containment radius $\Psi_{68\%}$ can be assessed. For values $\beta \lesssim 0.5^\circ$ and reconstructed energies above ~ 10 TeV, the relation between β and $\Psi_{68\%}$ is close to what is expected from a two-dimensional Gaussian function. At lower energies and for higher values of β , the value of $\Psi_{68\%}$ becomes significantly higher than the Gaussian expectation up to a factor 2, which motivated the choice of the maximum value $x = 2.0$. The scan on the x parameter is then an empirical way to take into account this complicated behavior while still using the reconstruction quality information of ANTARES neutrinos on an event-by-event basis. As a consequence, the p -value obtained with this method needs a trial factor correction.

A possible correlation between the radio flux density and neutrino emission is evaluated by performing an additional scan on the radio flux density $S_{8\text{GHz}}$: VLBI blazars are kept in the sample if they satisfy $S_{8\text{GHz}} > S_{\text{min}}$, and the value of S_{min} is

varied in the range $[0.15; 5.0]$ Jy. The maximum radio flux density of 5.0 Jy is chosen so that at least 10 sources are still included in the blazar catalog used for the correlation with neutrino events.

The results of the counting analysis are illustrated in Figures 2 and 3. When using the full VLBI catalog, the one-dimensional scan shows an absolute minimum for $x = 0.82$, where $n_{\text{obs}} = 469$ pairs are observed in the data, while $n_{\text{exp}} = 410.4$ are expected on average from random simulations (59 pairs in excess). The associated pretrial p -value is $p = 2.5 \times 10^{-3}$ (3.0σ), leading after correction to a posttrial p -value of $P = 3.0 \times 10^{-2}$ (2.2σ). Note that without performing a scan, the value $p(x = 1) = 5.0 \times 10^{-2}$ (2.0σ) would have been quoted instead.

As mentioned, the parameter x is introduced to (conservatively) consider a possible systematic difference in the angular resolution not included in the reconstruction algorithm. An x -value smaller than 1 could represent an overestimate of the systematic uncertainty in the reconstructed track, while $x > 1$ could represent an underestimate uncertainty. The value $x = 0.82$ found for the minimum seems to indicate that the angular systematic uncertainty β Adrian-Martinez et al. (2013) is slightly overestimated. However, as the position of this scan minimum is subject to fluctuations, this deviation of x from 1 is not significant enough to conclude that the reconstruction performance behaves better than expected from Monte Carlo simulations Albert et al. (2021b).

The search for a correlation with radio flux density with the two-dimensional scan (x, S_{min}) is shown in Figure 3. The absolute minimum is found for $x = 0.82$ and $S_{\text{min}} = 0.15$ Jy, with a pretrial p -value of $p(S > 0.15 \text{ Jy}) = 2.5 \times 10^{-3}$ and a posttrial $P(S > 0.15 \text{ Jy}) = 0.26$. This minimum corresponds to

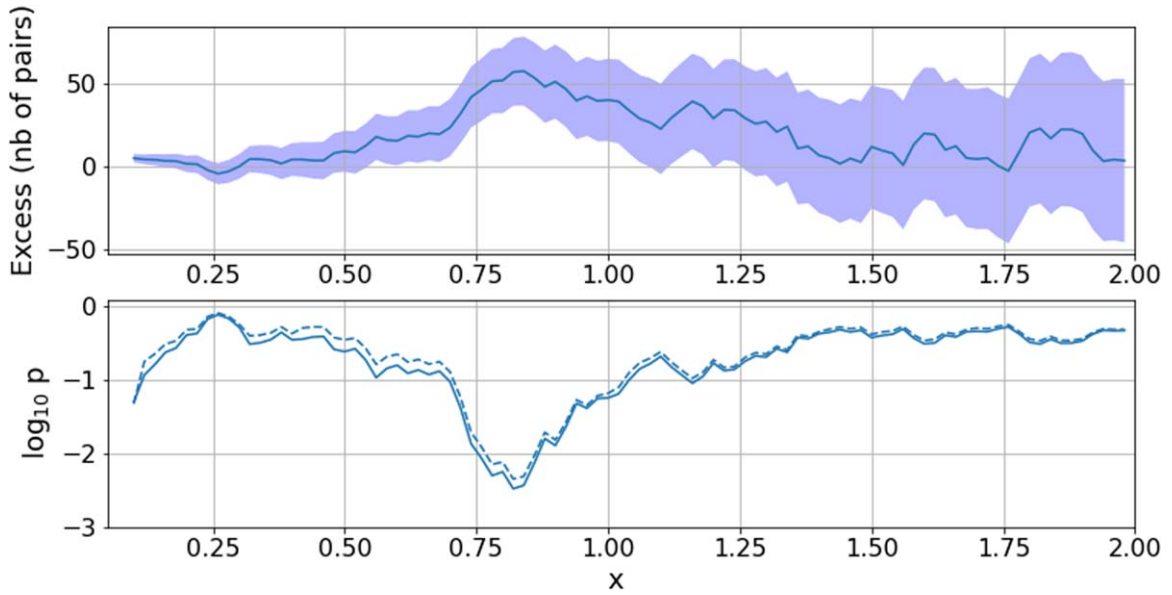


Figure 2. Result of the counting analysis with the VLBI blazar catalog. The top and bottom panels show, as a function of the parameter x (defined in the text), the observed excess of pairs relative to random expectations and the pre-trial p -value, respectively. In the top panel, the blue band shows the $\pm 1\sigma$ confidence interval. In the bottom panel, the dashed curve shows the p -value obtained when excluding blazars with $S > 3.68$ Jy from the catalog (see text).

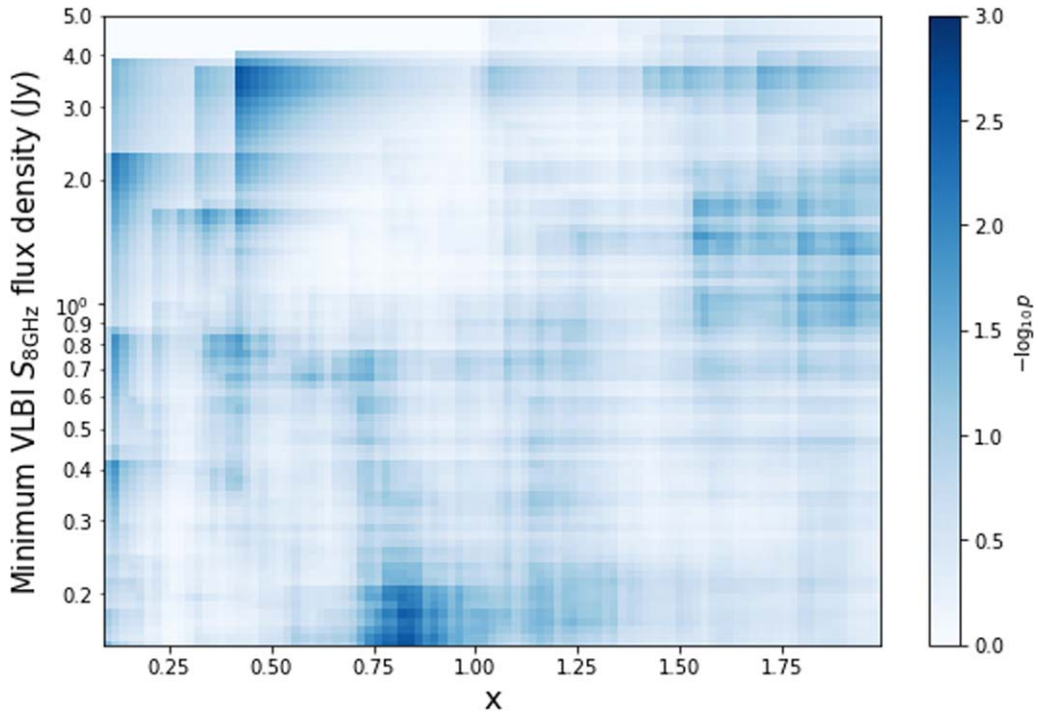


Figure 3. Result of the two-dimensional scan over the radio flux density $S_{8\text{GHz}}$ and parameter x . The color code indicates the pre-trial p -value.

the previous findings of the one-dimensional scan and is obtained for the lowest value of the flux density cut, meaning that the whole VLBI blazar catalog is included.

A local minimum is also visible for $x = 0.42$ and $S_{\text{min}} = 3.68$ Jy, with a pre-trial p -value of $p(S > 3.68 \text{ Jy}) = 2.7 \times 10^{-3}$. This excess is mainly driven by three blazars: J0609–1542 and J1743–0350, which have one very close ANTARES track (less than $0^\circ.2$ away), and J0538–4405, which has two events at $0^\circ.4$ distance. These sources are not found in the search for neutrino flares presented in Section 6, as only one neutrino is contributing for J0609–1542 and J1743–0350, and the two

events located around J0538–4405 are separated by more than 6.5 yr in time.

When accounting for the trial factors, the significance of this excess is $P(S > 3.68 \text{ Jy}) = 0.28$. In addition, as can be seen in Figure 2 (dashed line), when excluding the blazars with $S > 3.68$ Jy from the catalog, the position of the minimum stays the same, and the pre-trial p -value is only slightly increased, $p = 4.5 \times 10^{-3}$. These results indicate that the excess in the counting of neutrino–blazar pairs is not induced by a small number of very high flux sources in the VLBI catalog.

5. Time-integrated Likelihood Analysis

A time-integrated likelihood analysis very similar to the one reported in Albert et al. (2021a) is performed, making use of more information about the ANTARES detector response than the one used in the simple counting method. The likelihood of the null hypothesis H_b , where only background is present, is compared with an alternative hypothesis H_{s+b} , where signal events coming from blazars are present in the data.

The neutrino signal events are assumed to come from blazars in proportion to their measured VLBI flux density $S_{8\text{GHz}}$, with an energy spectrum modeled as a pure power law $E^{-\gamma}$. The analysis is performed for a fixed value of the spectral index γ and repeated for values $\gamma \in [1.8; 2.6]$ in 0.1 steps. This range includes the value predicted by the candidate acceleration mechanism ($\gamma = 2.0$) and the softer best-fit spectral indices measured by the IceCube Collaboration for the diffuse neutrino flux ($\gamma = 2.37$, Abbasi et al. 2022b; $\gamma = 2.53$, Aartsen et al. 2020) and for TXS 0506+056, a blazar showing evidence for neutrino emission ($\gamma = 2.1$ and 2.2; Aartsen et al. 2018a).

The likelihood is written as

$$\ln \mathcal{L}_{s+b} = \sum_i^N \ln(\mu_s S_i + \mu_b B_i) - \mu_s - \mu_b, \quad (1)$$

where N is the total number of observed tracklike events, S_i is the probability density function (PDF) of the signal, and B_i is the background one. The free parameters are the estimated number of signal, μ_s , and background, μ_b , events. The expression of the background-only likelihood \mathcal{L}_b is simply obtained by setting $\mu_s = 0$ in Equation (1).

The test statistics Q is defined as a likelihood ratio,

$$Q = 2 \ln \left[\frac{\max(\mathcal{L}_{s+b})}{\max(\mathcal{L}_b)} \right], \quad (2)$$

where the likelihoods defined in Equation (1) are maximized with respect to the free parameters μ_s and μ_b . In practice, as the background-only term \mathcal{L}_b is maximal when $\mu_b = N$, the numerical procedure of likelihood maximization has to be performed only for the \mathcal{L}_{s+b} term.

The core ingredients of the likelihood analysis are the signal and background PDF, which are written as the product of a spatial and an energy term,

$$S_i = f_s(\alpha_i, \delta_i, \beta_i, E_i) g_s(E_i) \quad \text{and} \quad B_i = f_b(\delta_i, E_i) g_b(E_i), \quad (3)$$

where (α_i, δ_i) are the equatorial coordinates, β_i is the angular uncertainty, and E_i is the estimated energy of the i th neutrino candidate.

The energy-dependent part of the signal PDF, $g_s(E)$, is computed using Monte Carlo simulations by building a histogram of the reconstructed energies E of tracklike events when assuming a pure power-law $E_{\text{true}}^{-\gamma}$ distribution of the true neutrino energies E_{true} . The background PDF, $g_b(E)$, is similarly obtained by building a histogram with Monte Carlo simulations, where the atmospheric neutrino fluxes (conventional+prompt components) and atmospheric muon fluxes are taken into account (see Albert et al. 2018c for details).

The spatial term $f_b(\delta_i, E_i)$ for the background is considered to be independent of the R.A. α . Indeed, the ANTARES data set has been obtained by accumulating 15 yr of quasi-continuous measurement; therefore, the nonuniformity of the detector

exposure in local coordinates is averaged out by the rotation of the Earth, leading to a flat R.A. distribution of events. In practice, the value of the background spatial term $f_b(\delta_i, E_i)$ is estimated by a linear interpolation within a two-dimensional $(\sin \delta, E)$ histogram built from Monte Carlo simulations.

The spatial signal term is obtained by summing over all the individual blazar contributions,

$$f_s(\alpha_i, \delta_i, \beta_i, E_i) = \frac{1}{\sum w_j} \sum_{j=1}^{N_{\text{sources}}} w_j \mathcal{F}(\Psi_{ij}, \delta_i, \beta_i, E_i) \quad w_j = w_j^{\text{model}} \mathcal{A}(\delta_j), \quad (4)$$

where $\mathcal{F}(\Psi_{ij}, \delta_i, \beta_i, E_i)$ is the ANTARES point-spread function (PSF) for tracklike events, defined as the probability density for the event direction to fall within a given angular distance from the true incoming direction. The PSF is a sharply decreasing function of the space angle Ψ_{ij} between the i th neutrino and the j th blazar and mostly depends, by decreasing order of importance, on the angular error β , the reconstructed energy E , and the decl. δ . The practical implementation of the PSF is obtained from Monte Carlo simulations by building two-dimensional histograms in (E, β) for eight separate bins of $\sin \delta$.

The weight of the j th blazar is proportional to its measured flux density $w_j^{\text{model}} = S_{8\text{GHz}}$ and corrected by the decl.-dependent acceptance $\mathcal{A}(\delta)$ of the ANTARES neutrino track sample (computed for the particular $E^{-\gamma}$ energy spectrum considered). For comparison, a basic scenario where all blazars have the same weight, $w_j^{\text{model}} = 1$, is considered.

The smallest p -value obtained with the time-integrated likelihood analysis is $p = 2.6 \times 10^{-2}$ (2.2σ) for the radio flux weighting hypothesis and $p = 7.6 \times 10^{-2}$ (1.8σ) for the equal weighting. These best fits are obtained with an $E^{-2.3}$ neutrino energy spectrum for both weighting schemes. This spectral index is also the best-fit value obtained with the latest ANTARES diffuse analysis Fusco & Versari (2019). This indicates that the candidate neutrinos in the direction of the VLBI blazars do not show a different energy spectrum than the diffuse astrophysical component extracted from the observed neutrino spectrum in the ANTARES data set.

As the studied spatial correlation between neutrino candidates and the VLBI blazars is not highly significant, upper limits at a 90% confidence level are reported in Figure 4. The upper limits are computed for the different spectral indices of the assumed power-law neutrino flux (thin violet lines), and their highest values as a function of the energy provide the most conservative limit curve (black solid curve in the figure). For comparison, the 68% allowed values from the ANTARES diffuse analysis are plotted (with a 15% systematic on the flux normalization included as in Albert et al. 2018c), together with the latest diffuse results from IceCube Abbasi et al. (2022c).

As mentioned at the beginning of this section, our best fit for a cosmic diffuse neutrino flux (orange dotted line) has a spectral index of $\gamma = 2.3$ and can be compared to the corresponding blazar upper limit (black line). For this particular value of γ , the ratio between the black and orange dotted lines is ~ 0.2 , implying that the VLBI blazars could not contribute to more than $\sim 20\%$ of our estimated total diffuse flux of cosmic neutrinos. However, as can be seen in Figure 4, when accounting for the wide 68% confidence interval on the ANTARES diffuse flux estimation, the total VLBI upper limit

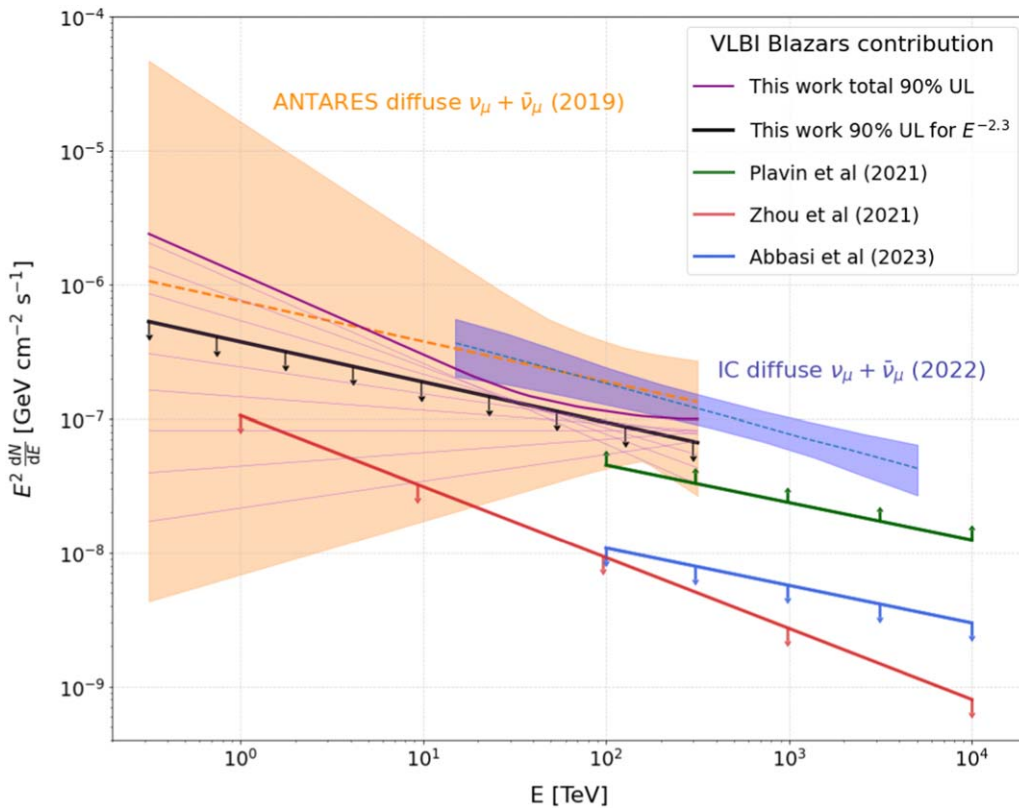


Figure 4. Upper limits on the one-flavor ($\nu_\mu + \bar{\nu}_\mu$) total neutrino flux from VLBI blazars, obtained through time-integrated likelihood analysis as a function of neutrino energy. Thin solid violet lines represent ANTARES limits for each tested spectral index (the thick black line highlights the $E^{-2.3}$ case), while the thick violet line depicts the uppermost envelope of individual spectral index limits, providing the most conservative upper-limit curve. For comparison, upper limits using IceCube data are shown (Zhou et al. 2021, thick red line; Abbasi et al. 2023d, thick blue line), together with the lower limit estimated in Plavin et al. (2021). The orange-shaded band represents the 68% confidence region for the diffuse flux measured by ANTARES (Fusco & Versari 2019), and the most recent IceCube diffuse ($\nu_\mu + \bar{\nu}_\mu$) flux estimation from Abbasi et al. (2022c) is displayed as a blue shaded band for the single power-law $E^{-2.37}$ hypothesis.

(violet line) only weakly constrains our measurement. When comparing with the most recent IceCube diffuse ($\nu_\mu + \bar{\nu}_\mu$) flux estimation from Abbasi et al. (2022c), our most conservative limit represents $\sim 65\%$ of the integrated energy flux measured by IceCube between 15 and 315 TeV (the energy range where there is an overlap).

To put our constraints of blazars' contribution to the neutrino flux into context, estimates from analyses based on IceCube measurements are also shown in Figure 4. These include upper limits obtained with different versions of the VLBI catalog, rfc2019c for Zhou et al. (2021) and rfc2022a for Abbasi et al. (2023d), and lower limits estimated in Plavin et al. (2021) with version rfc2019c. The apparent tension between these estimates stems from differences in the assumptions put into corresponding statistical analyses; see discussions in Abbasi et al. (2023d) and Plavin et al. (2023). Utilizing observational data from other neutrino telescopes is crucial for independent checks of such assumptions, especially considering the statistical nature of all current associations.

6. Time-dependent Likelihood Scan

The time-dependent scan looks for neutrino flares from the direction of the selected radio-bright blazars and also relies on an unbinned maximum-likelihood method. Since this search looks for clustering of events in space and time, the knowledge of the detection time of the selected events is included in the likelihood and combined with the spatial and energy information. This is achieved by multiplying the signal and background PDFs of

Equation (3) by a time-dependent term. Unlike in the time-integrated analysis, the likelihood is maximized independently at the position of each investigated source, meaning that each source is analyzed separately. Therefore, the spatial signal term of Equation (4) simplifies into $f_s(\alpha_i, \delta_i, \beta_i, E_i) = \mathcal{F}(\Psi_{ij}, \delta_i, \beta_i, E_i)$. Regarding the signal time PDFs, two generic time profiles describing a temporary increase in neutrino emission—a Gaussian profile and a box profile—are tested. They are defined as

$$\begin{aligned} \mathcal{S}_{\text{Gaussian}}^{\text{time}}(t_i) &= \frac{1}{\sqrt{2\pi}\sigma_t} e^{-\frac{(t_i - T_0)^2}{2\sigma_t^2}}, \mathcal{S}_{\text{box}}^{\text{time}}(t_i) \\ &= \begin{cases} \frac{1}{2\sigma_t}, & \text{if } [T_0 - \sigma_t] \leq t_i \leq [T_0 + \sigma_t]; \\ 0, & \text{otherwise;} \end{cases} \end{aligned} \quad (5)$$

with t_i being the detection time of the neutrino candidate event i , and T_0 and σ_t being the unknown central time and duration of the flaring emission, respectively, both fitted in the likelihood maximization. Given the small expected contribution of a cosmic signal in the overall data set, the background time profile is built using the time distribution of data events, ensuring a time profile proportional to the measured data. This PDF is computed by applying less stringent selection criteria than those of the final sample so as to avoid statistical fluctuations, using the same approach as in Albert et al. (2019).

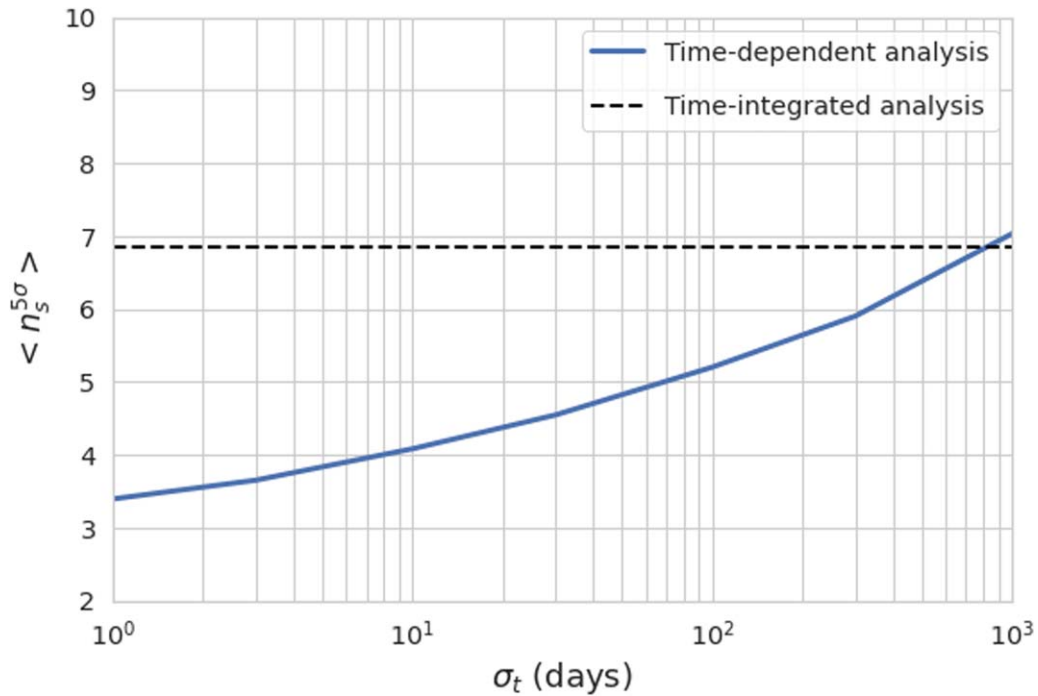


Figure 5. 5σ discovery potential in terms of mean number of signal events as a function of the simulated flare duration for the time-integrated analysis (dashed) and for the time-dependent analysis (solid). The simulated source is at a decl. of $\delta = -40^\circ$, and the flare is centered at T_0 [MJD] = 57000. Similar results are obtained for different source declinations and central times.

At the location of each investigated source, the likelihood is maximized, leaving as free parameters the number of signal events μ_s , the signal spectral index γ , the central time of the flare T_0 , and the flare duration σ_t . The procedure allows for a single flare per blazar to be fitted and, for the given best-fit flare (the flare with the highest Q), provides the best-fit values $\hat{\mu}_s$, $\hat{\gamma}$, \hat{T}_0 , and $\hat{\sigma}_t$. In the maximization, the spectral index can take values between 1.0 and 3.5. Concerning the time-dependent parameters, T_0 can vary over the time range of the investigated ANTARES data (from 2007 January 29 to 2020 February 29), while σ_t can take values between 1 and 2000 days.

The test statistic Q , similarly to the time-integrated analysis, is defined as the logarithm of the ratio between the likelihood evaluated with the best-fit values of the free parameters and the background-only likelihood. However, in this case, the likelihood ratio is multiplied by a penalty term for short flares, $\hat{\sigma}_t/\Delta T$, with ΔT being the allowed time range for T_0 . The purpose of the penalty term is to account for the larger trial factor that should be associated with short flares since a larger number of short flares than of long ones can be accommodated in a given time range, as described in Braun et al. (2010).

In order to estimate the p -value of the best flare for each investigated source, the observed Q -value is compared to the test statistic distribution obtained with background-only pseudo-experiments (PEs). In each PE, the analysis is performed on the data set randomized in R.A. to eliminate any local clustering due to potential sources keeping the corresponding source decl. In particular, the p -value is given by the fraction of background-like PEs with a value of the test statistic larger than the observed Q . The lowest obtained p -value identifies the most significant flare of the search. Finally, a trial correction that accounts for the fact that many candidates have been investigated is applied by comparing the lowest obtained p -value to the distribution of the smallest

p -values found when performing the same analysis on many background-only PEs.

Figure 5 shows the expected performance of this approach compared to that of the time-integrated analysis, i.e., when the time information of the events is not considered. The 5σ discovery potential $\langle n_s^{5\sigma} \rangle$ —defined as the mean number of injected signal events needed for a 5σ discovery in 50% of the PEs—is shown as a function of the duration of the flare. The time-dependent search performs better along almost the entire investigated range of flare durations, with an improvement in the discovery potential by a factor of ~ 2 achieved for flares as short as 1 day.

The search results in 18 sources showing a flare with a pretrial significance above 3σ for at least one of the tested time profiles. They are visualized in Figure 6 and listed in Table 1, together with the corresponding best-fit values of the free parameters. The most significant Gaussian (box) flare is found from the direction of J1355–6326 (correspondingly, J1826+1831), with a pretrial significance of 3.7σ (correspondingly, 3.3σ) in the two-sided convention. When accounting for the fact that multiple sources have been investigated, posttrial p -values of 29% and 84% are obtained for the best Gaussian and box flares, respectively. The result found for J1355–6326, with a best-fit flare duration of over 1000 days, is expected to be very close to the one that would have been obtained in a search for neutrino clustering in which the event time is not considered, as it can be derived from Figure 5. The weighted time distribution of the ANTARES events close to J1355–6326 and J1826+1831 is shown in Figure 7. Only tracklike (shower-like) events within a distance of 5° (10°) from the blazars are included in the plot. A higher weight is associated with events with smaller distances to the source and larger values of the energy estimator. Since the weight does not take into account the arrival time of the events, the best-fit flares do not necessarily cover in time the individual neutrino candidates

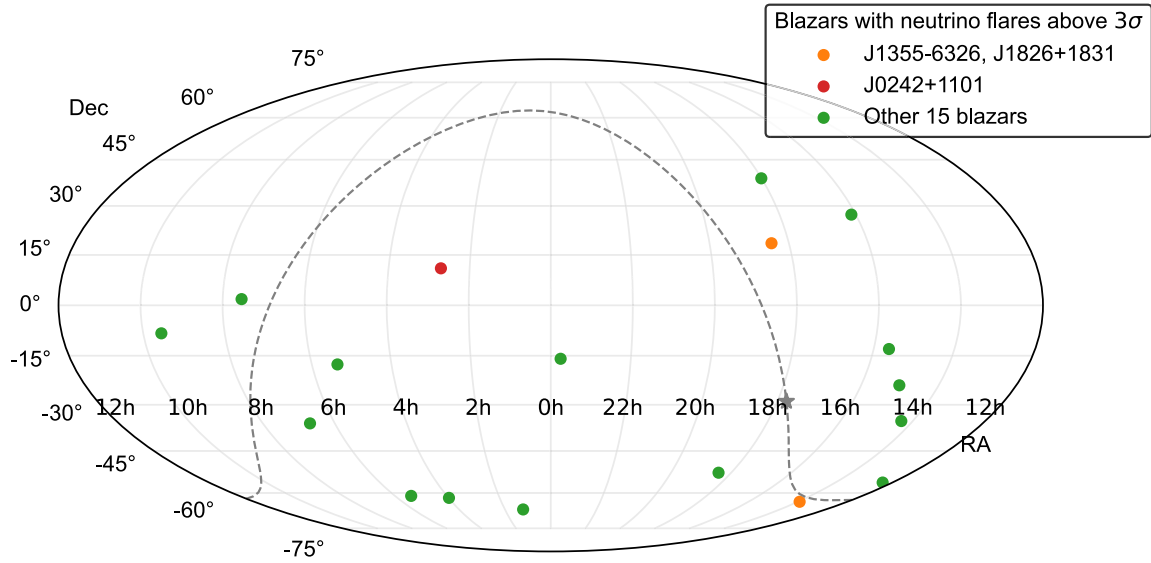


Figure 6. Sky map in equatorial coordinates showing the positions of the VLBI blazars coincident with the 3σ flares found in ANTARES data (orange dots). See Table 1 for a list of these flares. The two blazars with the most significant excesses are depicted in orange, while the red dot indicates the blazar studied in Section 7. The locations of the Galactic plane (dashed line) and Galactic center (star) are also shown.

Table 1
Results of the Time-dependent Likelihood Scan

Source			Results									
Name	δ (deg)	α (deg)	Gaussian-shaped Time Profile					Box-shaped Time Profile				
			\hat{T}_0 (MJD)	$\hat{\sigma}_T$ (days)	$\hat{\mu}_s$	$\hat{\gamma}$	p -value	\hat{T}_0 (MJD)	$\hat{\sigma}_T$ (days)	$\hat{\mu}_s$	$\hat{\gamma}$	p -value
J0112–6634	–66.6	18.1	58215	304	4.5	2.7	0.0026	58154	305	3.8	2.7	0.0097
J1355–6326	–63.4	208.9	56524	1041	7.9	2.8	0.00018	56091	905	6.0	2.9	0.0048
J0359–6154	–61.9	59.7	56316	78	5.4	3.5	0.0022	56321	112	5.7	3.5	0.0013
J0522–6107	–61.1	80.6	56221	42	4.6	3.4	0.0034	56232	59	4.9	3.4	0.0023
J1220–5604	–56.1	185.1	58406	18	2.8	2.6	0.00029	58413	22	0.4	2.2	0.0032
J1825–5230	–52.5	276.3	57265	600	5.4	2.7	0.0031	57188	959	5.5	2.7	0.0027
J0641–3554	–35.9	100.3	58084	16	2.9	3.0	0.0021	58081	19	3.0	3.0	0.0018
J1418–3509	–35.2	214.7	58120	11	3.3	2.9	0.0018	58121	14	2.9	2.8	0.0021
J1500–2358	–24.0	225.2	55846	4	3.7	2.3	0.0016	55847	6	3.7	2.2	0.0015
J0521–1737	–17.6	80.3	57332	1	2.0	1.9	0.0011	57333	1	2.0	1.9	0.0023
J2345–1555	–15.9	356.3	57653	460	3.2	2.6	0.0011	57784	404	2.4	2.7	0.0030
J1537–1259	–13.0	234.3	58201	46	2.6	2.0	0.0019	58201	55	2.7	2.0	0.0016
J0933–0819	–8.3	143.3	57411	533	3.1	2.0	0.0014	57128	697	2.9	2.0	0.0017
J0732+0150	1.8	113.1	55794	82	5.0	3.5	0.0010	55854	61	2.7	3.4	0.033
J0242+1101	11.0	40.6	56676	311	5.4	2.2	0.0060	56586	451	6.6	2.6	0.0021
J1826+1831	18.5	276.6	57672	151	2.9	2.5	0.0015	57636	178	3.0	2.5	0.0010
J1606+2717	27.3	241.7	58793	1	1.0	1.0	0.00076	58793	1	1.0	1.0	0.0017
J1800+3848	38.8	270.1	56590	3	1.7	2.4	0.0024	56590	3	1.9	2.6	0.0021

Note. List of radio-bright blazars for which a pretrial significance above 3σ for at least one of the tested time profiles (Gaussian-shaped and box-shaped) has been obtained. The first three columns report the name and equatorial coordinates of the sources. The remaining columns summarize the results of the search in terms of the best-fit central time of the flare \hat{T}_0 , flare duration $\hat{\sigma}_T$, number of signal events $\hat{\mu}_s$, spectral index $\hat{\gamma}$, and pretrial p -value for the Gaussian-shaped and box-shaped signal time profiles. The most significant flare found assuming each of the considered time shapes is highlighted in bold.

with the highest weight. Indeed, as the algorithm searches for clustering of events in space and time, an ensemble of multiple events detected at close times rather than a single high-weight event is identified as a flare.

While none of the investigated sources alone is observed at a significant detection level when accounting for trials, a further study is performed to check for the presence of a cumulative excess. By performing background PEs in which the same source catalog is targeted, it is found, as shown in Figure 8, that the probability of finding 18 or more sources with a pretrial

significance greater than 3σ is 1.4% (2.5σ). This result provides an additional hint to the time-independent analysis, that a fraction of the blazars contained in the VLBI catalog could be neutrino emitters.

7. Multimessenger Flare Comparison

As a follow-up study of the findings of this analysis, the obtained best-fit neutrino flares have been compared to the radio light curves produced by the Owens Valley Radio

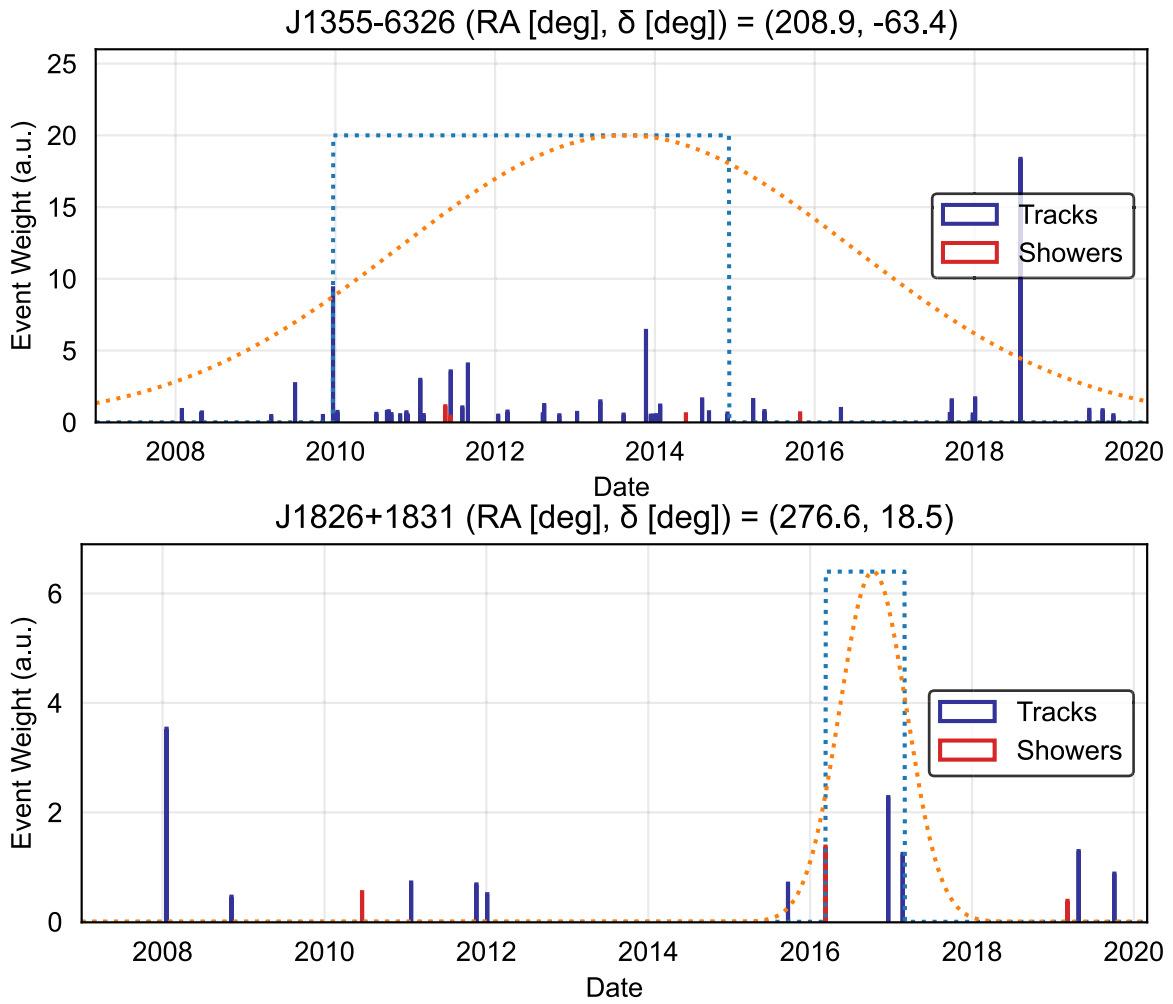


Figure 7. Weighted time distribution of the ANTARES events close to the location of J1355–6326 (top) and J1826+1831 (bottom). The dotted box and Gaussian time profiles have been drawn using the best-fit values of $\hat{\sigma}_T$ and \hat{t}_0 found in each case and reported in Table 1. Tracks (showers) are shown in blue (red).

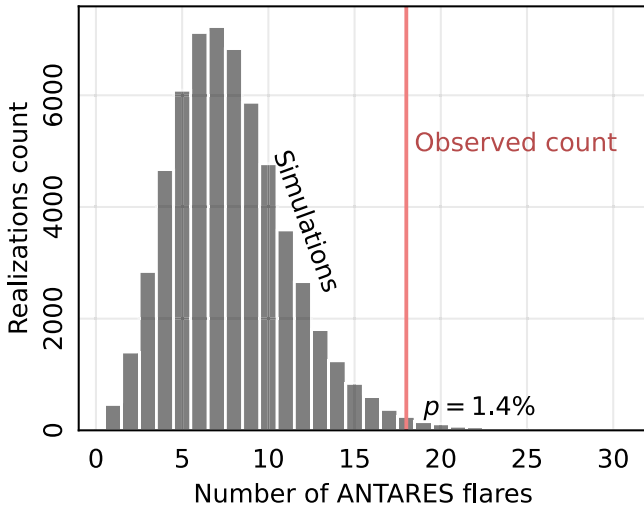


Figure 8. Cumulative excess of 3σ flares found in ANTARES data. The vertical line indicates the observed count, while the histogram represents the number of sources in random realizations. The probability of observing 18 or more sources with a pretrial flare significance above 3σ is 1.4%.

Observatory (OVRO; Richards et al. 2011) for those sources of Table 1 for which radio data are available. Only for the source J0242+1101 (PKS 0239+108) has a notable overlap in

time been found between the best-fit neutrino flare identified in this analysis and its largest flare observed in radio, as shown in Figure 9. In view of this observation, the time distribution of the public data of the Fermi Large Area Telescope (LAT) γ -ray telescope and the IceCube neutrino telescope compatible with the direction of J0242+1101 have also been studied. Figure 9 also reports the adaptive binned γ -ray light curve, obtained from Fermi data using the method described in Lott et al. (2012) and Kramarenko et al. (2022). Remarkably, the most significant Fermi γ -ray flare for this blazar happened during the flaring emission detected in radio and the period highlighted by the ANTARES analysis. Note that the γ -ray flare peak preceding radio is a typical scenario explained by synchrotron self-absorption of the jet base; this locates the γ -ray emission region close to the jet base Pushkarev et al. (2010), Kramarenko et al. (2022). The time distribution of the IceCube tracklike events in the 10 yr point-source sample IceCube Collaboration (2021) with a direction compatible with the blazar position within the 50% angular error reported by the IceCube Collaboration is also shown. Only events with an angular uncertainty contour smaller than 10 deg^2 are depicted. While there is no evidence of time clustering of the IceCube events, a ν_μ -induced track with the notable high energy of 50 TeV was detected during the flare, its reported angular uncertainty radius being $1^\circ.4$. Furthermore, it is worth reporting

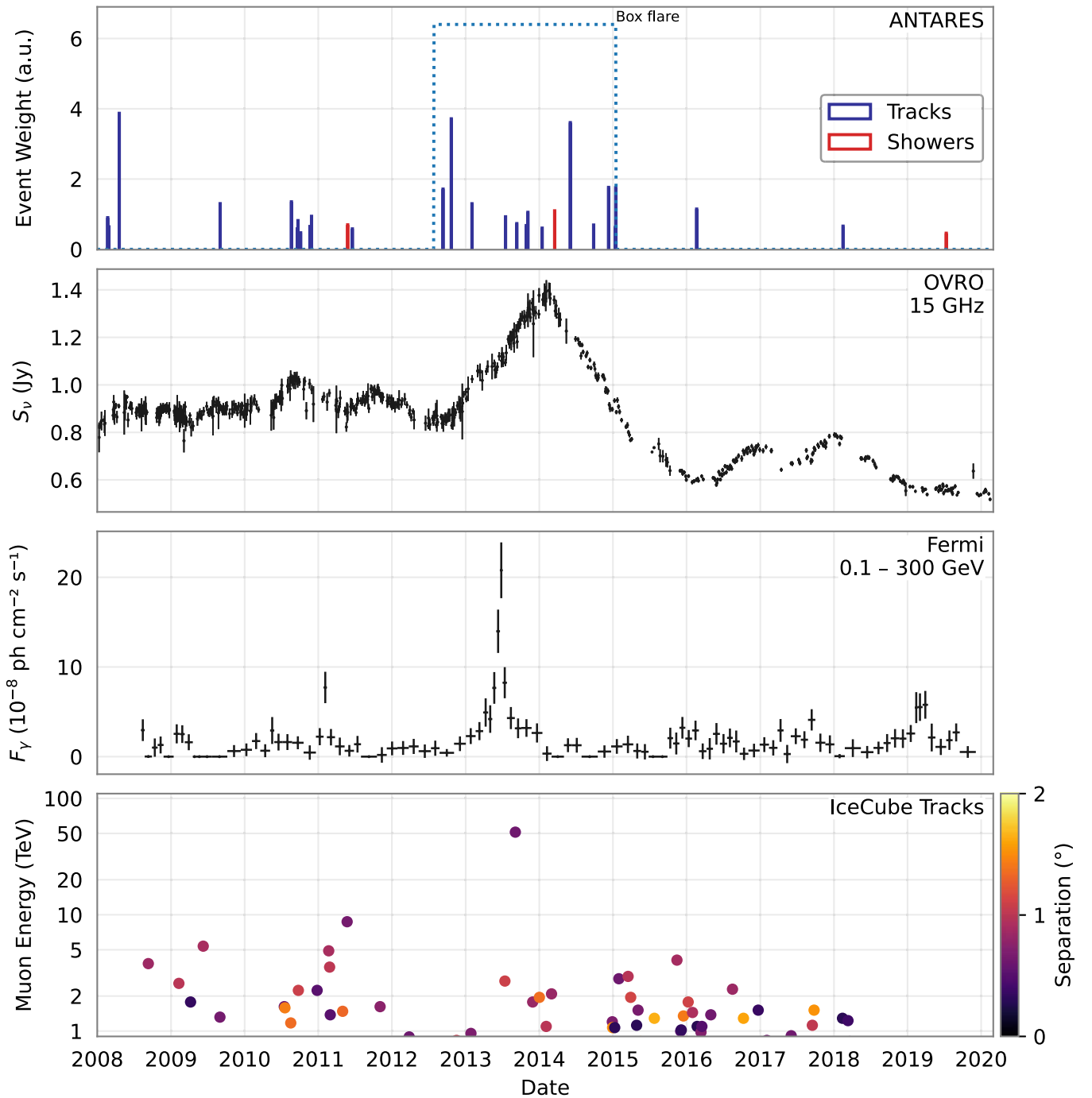


Figure 9. Multimessenger light curves from the direction of the blazar J0242+1101 as a function of time since 2008. Top panel: weighted time distribution of the ANTARES tracklike (shower-like) events within 5° (10°) from this object. The box profile has been drawn using the best-fit values of $\hat{\delta}_r$ and \hat{T}_0 found in this analysis. Second panel: OVRO radio light curve. Third panel: adaptive binned γ -ray light curve obtained from Fermi LAT data. Bottom panel: weighted time distribution of the IceCube tracklike events closer to J0242+1101 than their 50% angular uncertainty. The applied weight corresponds to the energy of each event. The color scale indicates the event angular distance from the source.

that three IceCube alerts Abbasi et al. (2023e), namely, 131165:9342044, 129933:32926212, and 128672:38561326, have a likelihood best-fit direction that lies at a distance of $1^\circ.4$, $1^\circ.5$, and $1^\circ.6$, respectively, from J0242+1101. However, their detection date is subsequent to the one of the flare discussed here.

The neutrino-radio- γ flare coincidence in J0242+1101 is an a posteriori nonblind finding. It is still instructive to evaluate how likely such a correlation is to arise by chance. This study is conducted by means of PEs. In each PE, the time-dependent

search described in Section 6 is performed on a mock data set obtained by scrambling the real data in R.A. Each PE results in a list of fake best-fit neutrino flares, similar to Table 1. The chance probability of the correlation is then calculated by comparing such fake best-fit flares with the available OVRO and Fermi light curves as the percentage of flares fulfilling the following criteria:

1. the global maximum of their radio/ γ light curve falls within the ANTARES flare duration, $\hat{T}_0 \pm \hat{\delta}_r$, and

2. that maximum is at least as high as for J0242+1101, compared to the median flux of the same blazar; this corresponds to maximum-to-median ratios above 1.6 for radio and above 3.5 for γ .

Thanks to the OVRO and Fermi observatories, both radio and γ -ray light curves are available for hundreds of blazars: the CGRaBS OVRO sample Hovatta et al. (2021) and weekly curves from the Fermi LAT light Curve Repository⁵⁹ Abdollahi et al. (2023). There are 335 blazars in the intersection of these samples.

The outcome of this study indicates that it is relatively rare to find even a single matching blazar with the abovementioned characteristics; it appears in only $p = 0.5\%$ of random realizations, 4% for either radio or γ -rays separately. This fraction of $p = 0.5\%$ is the p -value, the chance coincidence probability of observing this kind of temporal neutrino-electromagnetic correlation. Given that the J0242+1101 analysis is a posteriori, these findings should be considered as hints to be tested further when more data become available.

8. Summary

A search for associations between 3411 radio-bright blazars of a complete VLBI flux-density-limited all-sky sample and an ANTARES neutrino event sample has been performed.

A time-integrated association search was conducted with pair-counting and likelihood-based approaches, using only the tracklike neutrino candidates. The pair-counting method finds an excess of 59 neutrino–blazar pairs with a posttrial p -value of 0.03 (2.2σ). The likelihood-based method finds a similar p -value of $p = 0.03$ for an energy spectrum of $E^{-2.3}$ and with the assumption of a neutrino flux proportional to the VLBI flux density. Upper limits on the neutrino flux from VLBI blazars are computed for different values of the spectral index $E^{-\gamma}$, mildly constraining the blazar contribution to $\sim 65\%$ of the high-energy neutrino diffuse flux measured by the IceCube Collaboration and also supported by ANTARES data.

The time-dependent search for flares, conducted using an unbinned maximum-likelihood method and combining tracklike and shower-like samples, finds 18 sources with neutrino flares above 3σ (pretrial). The two most significant flares come from the blazars J1355–6326 (3.7σ pretrial) and J1826+1831 (3.3σ pretrial); see Table 1. However, neither is significant alone after correcting for multiple trials. A cumulative effect is detected with $p = 0.014$ (2.5σ). This could be a hint of a population of blazars producing neutrinos with strong variations of the flux density.

A notable temporal correspondence between the neutrino flare from the direction of the J0242+1101 blazar and the most prominent wide-band electromagnetic flare of that source is found. The chance probability of such a coincidence between neutrino emission, radio, and γ -ray light curves is $p = 0.5\%$. This is a post hoc estimate that could be a hint of a connection between neutrino and electromagnetic emission. More observational data are required to verify the correlation more robustly and look for other similar coincidences.

The first results on associating ANTARES neutrinos with blazars uniformly selected by their bright radio emission are presented in this paper. Blazar neutrino emission appears highly variable and is likely to correlate with electromagnetic





flares. Still, the situation is far from being clear, and other classes of neutrino sources should contribute; the neutrino sky can be diverse, including a Galactic component. All neutrino observatories, IceCube, KM3NeT, and Baikal-GVD, are continuously improving to provide more detections with better directional accuracy and reliability. A strengthening of the observed correlation between blazars and neutrinos could be expected in the coming years. Radio observational programs are ongoing to aid in reliable identification of coincidences and better understanding of associations.

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