

1 **Mixed microalgae culture for ammonium removal in the absence**
2 **of phosphorus: Effect of phosphorus supplementation and process**
3 **modeling**

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16 **ABSTRACT**

17 Microalgal growth and ammonium removal in a P-free medium have been studied in two
18 batch photobioreactors seeded with a mixed microalgal culture and operated for 46 days. A
19 significant amount of ammonium ($106 \text{ mgN-NH}_4 \cdot \text{l}^{-1}$) was removed in a P-free medium,
20 showing that microalgal growth and phosphorus uptake are independent processes. The
21 ammonium removal rate decreased during the experiment, partly due to a decrease in the
22 cellular phosphorus content. After a single phosphate addition in the medium of one of the
23 reactors, intracellular phosphorus content of the corresponding microalgal culture rapidly
24 increased, and so did the ammonium removal rate. These results show how the amount of
25 phosphorus internally stored affects the ammonium removal rate. A mathematical model was
26 proposed to reproduce these observations. The kinetic expression for microalgae growth
27 includes a Monod term and a Hill's function to represent the effect of ammonium and stored
28 polyphosphate concentrations, respectively. The proposed model accurately reproduced the
29 experimental data ($r=0.952$, $P\text{-value}<0.01$).

30 **Keywords**

31 Ammonium removal; microalgae; mathematical modeling; phosphate; wastewater.

32 **HIGHLIGHTS**

- 33
- Ammonium removal takes place uncoupled from phosphate uptake
 - Ammonium removal rate depends on the amount of phosphorus internally stored
 - Effect of stored polyphosphate on ammonium removal modelled using Hill's equation
 - Enhanced ammonium removal at polyphosphate content higher than 2.2% dry weight
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38 1. INTRODUCTION

39 Interest on microalgae has increased during the last decades as they constitute a promising
40 alternative for obtaining value-added products and biofuels such as biodiesel, biohydrogen
41 biogas or biocrude. Moreover, microalgal systems for wastewater treatment have long been
42 proposed and studied [1]. These systems range from open-pond cultures to closed
43 photobioreactors [2] and focus primarily on the removal of inorganic nutrients such as
44 ammonium, nitrate and phosphate.

45 Several studies have proved the suitability of microalgal cultures for nutrient removal in
46 diverse wastewaters. These studies, which showed different degrees of nutrient removal
47 efficiencies, generally agree that the most important advantages of microalgae utilization for
48 this purpose are CO₂ abatement and the possibility of reusing biomass as fertilizer or as
49 renewable source of energy [3-5]. On the other hand, the process spares the otherwise
50 necessary cost of nutrients for algae cultivation. Currently, a rather extended opinion in the
51 scientific community is that the production of algae-based biofuels, at least in the short-term,
52 is neither economically nor energetically feasible without simultaneous wastewater treatment
53 [6].

54 Phosphorus is an essential component of microalgae. According to the Redfield ratio [7], it
55 constitutes 0.87% of its dry weight. Phosphorus is present in basic cell constituents such as
56 phospholipids, nucleic acids or nucleotides. It can also be accumulated to higher levels inside
57 the microalgal cells, where inorganic polyphosphate serves as reservoir. As reviewed by
58 Powell et al. [8], there are two mechanisms involved in this accumulation: over-
59 compensation, which occurs after re-exposure to phosphorus following a starvation phase, and

60 luxury uptake, where microalgae accumulate much more phosphorus than it is needed for
61 their survival without previous exposure to P-poor medium.

62 Different studies, which aimed at defining the polyphosphate accumulation and phosphate
63 uptake dynamics, have shown a relationship between phosphorus stress in the medium and
64 low polyphosphate content in the cells, together with recovery of polyphosphate levels after
65 addition of phosphorus [9-10]. It is also known that starvation enhances the phosphate uptake
66 rate. The effect of P-starvation on ammonium uptake rate is, however, less known. Previous
67 studies did not focus on the influence that polyphosphate content exerts on the nitrogen
68 uptake velocity, as these studies were not undertaken with a wastewater treatment approach.

69 In the wastewater treatment field mathematical models are useful tools for process design,
70 WWTP scale-up or upgrade, or water quality prediction. Up to now, microalgal growth
71 modelling has been tackled with a diversity of approaches. There are various examples of
72 different complexity-level models which determine phytoplankton evolution in the
73 ecosystems [11-13], content and evolution of intracellular components of interest such as
74 lipids or sugars [14], specific metabolism of single species [15], microalgal production inside
75 photobioreactors [16] or others.

76 The present work was designed to study the ammonium removal process in a phosphate-free
77 medium and the relationship between the microalgal intracellular phosphorus content and the
78 ammonium removal rate, with a view to designing suitable strategies for wastewater
79 treatment. Therefore it is also the aim of this work to define a kinetic expression for
80 microalgae growth considering the effect of ammonium concentration in the medium and the
81 amount of internally stored polyphosphate on the rate of this process. To this aim, a
82 mathematical model considering microalgae growth and death was proposed and model

83 parameters were obtained by minimizing differences between experimental data and model
84 predictions. This model should be useful for prediction of ammonium removal rates in
85 wastewater treatment systems.

86 A microalgal culture was fed only with ammonium in a lab-scale photobioreactor (PBR) and
87 afterwards separated into two identical PBRs. Phosphate was supplied only to one of them.
88 Nutrient uptake kinetics of the two PBRs were studied, as well as biomass composition (%N
89 and %P). Microalgae production-in terms of chemical oxygen demand and suspended solids-
90 was assessed. The experimental data obtained was successfully reproduced by the proposed
91 model. This model can be useful for designing strategies and predicting the behavior of
92 wastewater treatment systems where nutrient removal is achieved by microalgal growth.

93 **2. MATERIALS AND METHODS**

94 **2.1. Experimental setup**

95 Three identical PBRs were used in this study (*initial reactor, Nitrogen Only Reactor and*
96 *Nitrogen and Phosphorus Reactor*, as it will be explained in section 2.2). Each PBR consisted
97 of a cylindrical, transparent methacrylate tank (20 cm internal diameter) with a total volume
98 of 10 liters (see fig. 1a). The PBRs were closed and the algae culture was mixed by recycling
99 the headspace gas through four fine bubble diffusers mounted at the bottom. Both PBRs were
100 equipped with electronic sensors in order to obtain online measurements of conductivity,
101 oxidation reduction potential, temperature, pH and dissolved oxygen. The probes were
102 connected to a multiparametric analyzer (CONSORT C832, Belgium) and an oximeter (Oxi
103 320, SET WTW, Germany), respectively. These devices were in turn connected to a PC for
104 data monitoring and storage. Data sampling was conducted every 60 s.

105 pH in the PBRs was maintained around 7.5 to avoid undesirable processes such as phosphate
106 precipitation and free ammonia stripping. Pure CO₂ (99.9%) from a pressurized cylinder was
107 injected into the gas flow whenever pH exceeded the setpoint of 7.5. Recycling gas from the
108 headspace contributes to minimize the CO₂ requirements for pH control. Since the reactors
109 were closed CO₂ stripping was also minimized but since they were not hermetically sealed
110 extreme overpressure and overaccumulation of oxygen were avoided. Four arrays of 3 vertical
111 fluorescent lamps (Sylvania Grolux, 18 W) 10 cm apart from each other continuously
112 illuminated each PBR from a minimum distance of 10 cm. Photosynthetically active radiation
113 (PAR) of $153 \pm 16 \mu\text{E m}^{-2} \text{s}^{-1}$ was measured at the surface of the reactors as the arrow in fig.
114 1b) indicates. The PBRs were placed inside a climatic chamber with air temperature control
115 set to 20 °C. Due to the constant illumination the temperature in the culture resulted in 25.5
116 °C.

117 A phosphate-free medium, adapted from [17] was used in this study, one litre of which was
118 composed of 115 g (NH₄)₂SO₄, 150 mg CaCO₃, 400 mg CaCl₂·H₂O, 400 mg Na₂SeO₃·5H₂O,
119 350 mg MgSO₄·7H₂O, 54 mg (NH₄)₆Mo₇O₂·4H₂O, 30 mg ZnCl₂, 30 mg HBO₃, 30 mg
120 NiCl₂·6H₂O, 18 mg CuCl₂·2H₂O, 12 mg K₂SO₄, 1.2 mg FeCl₃·4H₂O, 1.2 mg CoCl₂·6H₂O,
121 0.6 mg EDTA, 0.3 mg MnCl₂·4H₂O.

122 **2.2. Operation**

123 7L of a microalgal culture was maintained for 19 days in ammonium-rich and phosphate-free
124 medium in a lab-scale PBR as described in section 2.1, called *initial reactor*. Ammonium in
125 the form of (NH₄)₂SO₄ was manually added at the beginning of the experiment and when its
126 concentration dropped below 4 mg NH₄-N·l⁻¹ (day 7). On day 19, when ammonium
127 concentration had reached again 4 mg NH₄-N·l⁻¹, the 7 L culture was split into two PBRs,

128 with a working volume of 3.5 L each. These two PBRs will henceforth be called *NOR*
129 (*Nitrogen Only Reactor*) and *N&PR* (*Nitrogen and Phosphorus Reactor*) and were not carried
130 out in duplicate. Immediately after the splitting, ammonium in the form of $(\text{NH}_4)_2\text{SO}_4$ was
131 added into *NOR*, reaching a concentration of $28 \text{ mg NH}_4\text{-N}\cdot\text{l}^{-1}$, and phosphate in the form of
132 KH_2PO_4 was added into *N&PR*, reaching a concentration of $12 \text{ mg PO}_4\text{-P}\cdot\text{l}^{-1}$. From then on,
133 both reactors were operated for 27 days. Ammonium was added again in both reactors when
134 its concentration dropped below $4 \text{ mg NH}_4\text{-N}\cdot\text{l}^{-1}$ (day 29 in *NOR* and days 20, 22 and 29 in
135 *N&PR*)

136 **2.3. Microorganisms**

137 The *initial reactor* was seeded with microalgae isolated from the walls of the secondary
138 clarifier in the Carraixet WWTP (Valencia, Spain) and maintained in the laboratory under
139 semi-continuous feeding conditions with a cellular retention time of 4 days and continuous
140 illumination varying between 114 and $198 \mu\text{E m}^{-2} \text{ s}^{-1}$. The effluent of a submerged anaerobic
141 membrane bioreactor (SAnMBR, described in [18]) was used as growth medium. This
142 effluent displays a variable N/P ratio and has been proved to sustain algal growth [5].
143 Microalgae from the *Chlorococcum* genus together with cyanobacteria (*Spirulina* sp. and
144 *Pseudoanabaena* sp.) were identified as the main groups present.

145 **2.4. Analytical Methods**

146 Nutrient removal was evaluated by regular measurements of inorganic nitrogen and
147 phosphorus levels in the samples taken from the PBRs. Ammonium ($\text{NH}_4\text{-N}$), nitrite ($\text{NO}_2\text{-N}$),
148 nitrate ($\text{NO}_3\text{-N}$) and phosphate ($\text{PO}_4\text{-P}$) were determined according to Standard Methods [19]

149 (4500-NH₃-G, 4500-NO₂-B, 4500-NO₃-H and 4500-P-F, respectively) in a Smartchem 200
150 automatic analyzer (Westco Scientific Instruments, Westco). Total nitrogen in the algae
151 culture was measured using standard kits (Merck, Darmstadt, Germany, 100613). The acid
152 peroxodisulphate digestion method [19] was used for total phosphorus (TP) measurements.
153 The nitrogen content of the algae biomass was calculated as the difference between total
154 nitrogen and soluble nitrogen. Likewise, the phosphorus content of the algae biomass (total
155 suspended phosphorus, TSP) was calculated as the difference between total phosphorus and
156 orthophosphate concentration. Total and volatile suspended solids (TSS and VSS), as well as
157 chemical oxygen demand (COD) were determined according to Standard Methods [19].
158 All reported results were obtained from the previous analyses conducted in duplicate, except
159 for TSS and VSS where single analysis were made.

160 **3. RESULTS AND DISCUSSION**

161 **3.1. Nutrient removal**

162 The composition of the biomass in the *initial reactor* (7 L PBR) after inoculation is included
163 in table 1. According to [20], a phosphorus concentration in the biomass greater than 3%
164 suggests that phosphate luxury uptake has taken place. Therefore, the studied microalgal
165 biomass had stored, before the beginning of this experiment (during the cultivation under
166 semi-continuous mode), more phosphate than needed for growth.

167 Figs. 2a and 2b show the ammonium and phosphate evolution in the *NOR* and *N&PR*,
168 respectively. The experiment started in the 7 L *initial reactor* with biomass inoculation and
169 ammonium addition. The initial VSS and ammonium concentrations were 340 mgVSS·l⁻¹ and
170 32 mg NH₄-N·l⁻¹, respectively. Ammonium was added again after 7 days because its

171 concentration was below 4 mg $\text{NH}_4\text{-N}\cdot\text{l}^{-1}$. During this first period, which is common in both
172 graphs, phosphate concentration in the medium was zero (fig. 2). However, the microalgal
173 biomass removed a total of 58 mg $\text{NH}_4\text{-N}\cdot\text{l}^{-1}$.

174 Table 1 summarizes the evolution of TSS, VSS and suspended COD in the two reactors
175 during the experiment. Yield coefficients were calculated as the ratio between the amount of
176 biomass generated, measured as VSS and COD, and the ammonium removed.

177 VSS as well as suspended COD concentrations clearly increased in both reactors due to
178 microalgae growth (table 1). This increase was greater in *N&PR* since the amount of
179 ammonium and phosphate taken up was higher.

180 The biomass P content visibly decreased in the *initial reactor* and in the *NOR*, since the
181 microalgae growth took place using the internally stored polyphosphate. In the *N&PR* the
182 biomass P content sharply increased on day 19 (to a maximum of 2.8%) due to phosphorus
183 addition and immediate uptake. It decreased from then on for the rest of the experiment.

184 VSS yield coefficients are similar in the *NOR*, *N&PR* and in the *initial reactor*, whereas the
185 *N&PR* shows a slightly higher COD yield coefficient. It is hypothesized that this difference
186 could be attributed to the amount of phosphate taken up in *N&PR*: growth in *NOR* took place
187 without phosphate addition, like in the *initial reactor*, while in *N&PR* phosphate was
188 available and taken up by microalgae. However, analytical error of the performed
189 measurements (VSS and COD) hinders a clear conclusion on the subject. Biomass N content
190 obtained in the present work is in accordance with the general Redfield formulation [6] of
191 9.20 % ($0.092 \text{ gN}\cdot\text{g}^{-1}$).

192 **3.1.1. Nitrogen Only Reactor**

193 As shown in fig. 2a, microalgal ammonium uptake took place during all the experiment (46
194 days in total) in the *NOR*, without any external phosphate addition. This fact demonstrates
195 that ammonium and phosphorus uptake from the medium are two independent processes-in
196 the sense that one can occur without the other-, and clearly demonstrates that this microalgal
197 culture presents a great capacity for removing a high amount of ammonium in the absence of
198 phosphate in the medium. In this reactor a total of $106 \text{ mgN-NH}_4\cdot\text{l}^{-1}$ was removed without
199 phosphate in the culture medium.

200 After each ammonium addition its uptake took place at a constant rate until ammonium
201 concentration decreased to values around $10\text{-}13 \text{ mg NH}_4\text{-N}\cdot\text{l}^{-1}$ (Fig 2a. Filled lines turn into
202 dashed lines). The ammonium uptake rate significantly decreased when ammonium
203 concentrations were below this threshold. This low ammonium affinity observed in these
204 experiments should be taken into account in the design of PBRs for wastewater treatment
205 since large tank volumes or high hydraulic retention times will be required to obtain very low
206 ammonium concentrations. An exception to this was the last slope, when the constant rate was
207 not maintained below $20 \text{ mg NH}_4\text{-N}\cdot\text{l}^{-1}$. This exception will be discussed later in this section.
208 In the *NOR*, the ammonium uptake rate decreased with time throughout the experiment, likely
209 due to a decrease in the internally stored polyphosphate. The selfshading effect of the culture
210 also exerted its influence: biomass growth during the experiment led to a decrease in the
211 available light for microalgae even when the incident light remained constant. The calculated
212 ammonium removal rates (slopes shown in fig. 2a) decreased from $0.209 \text{ mgN}\cdot\text{l}^{-1}\cdot\text{h}^{-1}$ at the
213 beginning of the experiment to $0.09 \text{ mgN}\cdot\text{l}^{-1}\cdot\text{h}^{-1}$ at the end of the experiment. The specific
214 removal rate ($\text{mgN}\cdot\text{mgSSV}^{-1}\cdot\text{h}^{-1}$) (table 2) decreased during all the experiment. As no
215 phosphate was added at any time in the *NOR*, the P required for biomass growth could only be
216 taken from their internal P pool, which microalgae had accumulated during the previous phase

217 of cultivation under semicontinuous conditions. This internal polyphosphate consumption
218 during the experiment led to a decrease in the biomass P content, which reached 0.8% (0.008
219 $\text{gP}\cdot\text{gVSS}^{-1}$) at the end of the experiment (at day 46, see table 1), when ammonium removal
220 was taking place at a very slow rate. These results suggest the existence of a relationship
221 between the P content of the cells and the ammonium removal rate. The final biomass P
222 content is a very small value compared to the initial biomass composition (indicated in table
223 1). It is, according to [20] still higher than the minimum amount of internal phosphorus for
224 cell survival (between 0.2 – 0.4% in dry weight). In fact, [21] has shown a minimum
225 phosphorus content after starvation phase of 0.185 % (0.00185 $\text{gP}\cdot\text{g}^{-1}$ biomass). However,
226 approaching these minimum values of intracellular P content makes ammonium uptake rate
227 decrease. Around day 35 of the experiment, biomass in the *NOR* reached what seems quite a
228 critical P content. The ammonium uptake rate decreased to very slow values although
229 ammonium concentration was still 20 $\text{mgNH}_4\text{-N}\cdot\text{l}^{-1}$. At the same time, as table 1 shows,
230 suspended solids significantly increased along the experiment. Mutual shading of the
231 microalgae attenuates light in the PBR and microalgal growth was therefore also slowed down
232 for this reason.

233 **3.1.2. Nitrogen and Phosphorus Reactor**

234 Phosphate was added to *N&PR* on day 19 and reached a concentration of 11.7 $\text{mg PO}_4\text{-P}\cdot\text{l}^{-1}$.
235 Phosphate removal started immediately and its removal rate was 2 $\text{mg PO}_4\text{-P}\cdot\text{l}^{-1}\cdot\text{h}^{-1}$ until
236 phosphate concentration was nearly zero. This removal rate was very high, considering that
237 while the added phosphate was consumed, only 2.1 $\text{mg NH}_4\text{-N}$ were taken up by the
238 microalgae. The resulting N:P uptake ratio of 0.18 is very low, which is due to the phosphorus
239 starvation condition of the biomass. The majority of literature values on microalgal phosphate
240 uptake rate under balanced conditions are well below the presented value: [3] reported, for

241 *Chlorococcum*, a value of $0.0475 \text{ mg PO}_4\text{-P} \cdot \text{l} \cdot \text{h}^{-1}$ and [22] reported a value of $0.083 \text{ mg PO}_4\text{-P}$
242 $\cdot \text{l} \cdot \text{h}^{-1}$ for *Chlorella* sp. [23] reported for *Chlorella protothecoides* a closer value to the one
243 presented in this work of $1.3 \text{ mg PO}_4\text{-P} \cdot \text{l}^{-1} \cdot \text{h}^{-1}$.

244 *N&PR* was spiked with ammonium for a third, fourth and fifth time (fig. 2b). As previously
245 observed in the *NOR*, the ammonium uptake rates kept constant after the ammonium additions
246 but decreased when ammonium concentration in the medium reached values below 10-13 mg
247 $\text{NH}_4\text{-N} \cdot \text{l}^{-1}$. The value obtained for the ammonium removal rate after phosphate addition in the
248 *N&PR* showed a significant increase, due to a fast increase in intracellular phosphorus
249 concentration. Ammonium removal rate decreased along the rest of the experiment, as in
250 *NOR*, due to an increase of selfshading and a decrease in phosphorus content. At the end of
251 the experiment, ammonium concentrations reached lower values in *N&PR* than in *NOR*, and
252 still maintained a faster decreasing trend. At this point, P content of the biomass had reached
253 $0.017 \text{ gP} \cdot \text{gVSS}^{-1}$, which is higher than the biomass P content reached in *NOR* (0.008
254 $\text{gP} \cdot \text{gVSS}^{-1}$).

255 These results suggest that ammonium removal rate depends on the amount of phosphorus
256 stored in microalgae. Other authors modelled phytoplankton colimitation by nitrogen and
257 phosphorus [24] assuming that the maximum potential for N uptake takes place at high
258 concentrations of intracellular phosphorus, which is in accordance with the experimental
259 results obtained now in this work.

260 The specific ammonium uptake rates (with respect to VSS) obtained in the *N&PR* and the
261 associated biomass P content are shown in table 2, demonstrating how intracellular
262 polyphosphate content exerted a drastic and positive influence in the specific ammonium
263 removal rate: it decreased for the first 2 injections into *initial reactor*, continued decreasing

264 after the N injections into *NOR* and increased in *N&PR* after P addition, catching up with the
265 initial value of $6 \times 10^{-4} \text{ mgN} \cdot \text{mgSSV}^{-1} \cdot \text{h}^{-1}$. The addition of phosphorus in the medium was the
266 only difference between reactors.

267 The data shown in table 2 demonstrates therefore a high sensitivity of the specific ammonium
268 removal rate to microalgal P content: the higher the biomass P content the higher the specific
269 ammonium removal rate. However, the relationship between these variables is far from linear:
270 a sharp increase is observed in the specific ammonium removal rate when biomass P content
271 lies between 2.2 and 2.6%. After phosphate addition, the specific ammonium removal rate
272 rose from 2.11×10^{-4} for a P content of 2.2% to $6.07 \times 10^{-4} \text{ mgN} \cdot \text{mgSSV}^{-1} \cdot \text{h}^{-1}$ for a P content of
273 2.6%. When biomass P content decreased down to 2.0% due to microalgae growth without
274 phosphate addition the specific ammonium removal rate decreased to a value closed to that
275 previously observed. On the other hand, the selfshading effect due to biomass growth is
276 evidenced by the fact that almost no difference is observed between the ammonium uptake in
277 the *initial reactor* ($6.15 \times 10^{-4} \text{ mgN} \cdot \text{mgSSV}^{-1} \cdot \text{h}^{-1}$) and the “*recovered*” uptake rate in *N&PR*
278 ($6.07 \times 10^{-4} \text{ mgN} \cdot \text{mgSSV}^{-1} \cdot \text{h}^{-1}$) while biomass has quite a different P content (3.7 % and 2.6 %
279 P, respectively) and thus a faster ammonium uptake rate would be expected in *N&PR* if
280 intracellular content was to be the only influencing factor.

281 Comparison between the performances of both reactors shows that, for this microalgal
282 culture, below the threshold of around 2.2 – 2.6% of internal phosphorus the nitrogen uptake
283 rate decreases considerably and around 1% the microalgal culture is unsuitable for ammonium
284 removal applications due to the slow rate obtained. It has been demonstrated that under
285 phosphorus limitation the nitrogen uptake process takes place at much slower rates. The
286 obtained data also suggest that selfshading influences growth and nutrient uptake rates.

287 Therefore, these two factors (available light and available intracellular phosphorus content)
288 will be taken into account in the modelling step.

289 The present work has confirmed, for this microalgal culture, two main consequences of
290 phosphate addition to a P-starving culture:

291 -Phosphorus supplementation to the medium increases the ammonium removal rate by
292 increasing the amount of polyphosphate the biomass is able to accumulate.

293 -The added phosphate is removed at a fast rate due to the prior starving conditions. This could
294 be useful in the development of different strategies for wastewater nutrient removal and also
295 shows that biomass growth can still take place with low amounts of phosphorus, as already
296 reported by [25]. These authors proposed a P-starvation cultivation mode to minimize
297 phosphorus resource consumption. A low biomass P content might not be a drawback in some
298 cases, as for instance within a biorefinery concept, where ammonium removal rates are of no
299 concern, or substances of interest are not fertilizers.

300

301 **3.1.3. Biological nutrient removal**

302 All conclusions drawn from this study are based on the assumption that ammonium and
303 phosphate removal are solely due to microalgal uptake, as the pH control assures that neither
304 free ammonia stripping nor inorganic salts precipitation takes place. Further indication that no
305 inorganic precipitation occurred is the fact that the VSS percentage was always higher than
306 92% of TSS.

307 The algal culture studied was mainly composed of three species: *Chlorococcum* sp., *Spirulina*
308 sp. and *Pseudoanabena* sp. A pure culture has not been used in this study as the aim of this

309 work is to analyze the behavior of the culture which evolved from feeding a PBR with the
310 effluent of a SAnMBR [5]. The results obtained might be applied to those cultures with
311 similar species composition, since the results obtained in a microalga culture composed of
312 close-phylogenetic species with similar nutrient requirements and similar growth conditions
313 might reveal comparable absorption patterns. However, culture from different microalgae
314 clade might show different growth and ammonium removal rates.

315 On the other hand, the low nitrite and nitrate concentrations measured during all the
316 experiment (highest measured values were $2.2 \text{ mg NO}_2\text{-N}\cdot\text{l}^{-1}$ and $1.7 \text{ mg NO}_3\text{-N}\cdot\text{l}^{-1}$) indicate
317 no bacterial nitrification/denitrification activity took place. Constant soluble COD levels
318 (stable around $134 \text{ mg COD}\cdot\text{l}^{-1}$) support this hypothesis.

319 **3.2. Mathematical model**

320 **3.2.1. Proposed model**

321 A mathematical model focused on the kinetics of microalgal ammonium uptake was proposed
322 with the aim of representing the ammonium removal process observed in the PBRs. The main
323 characteristics of the proposed model are:

- 324 - Microalgal ammonium uptake rate does not depend on phosphate concentration in the
325 medium, since ammonium uptake still takes place in a phosphate depleted medium. The rate
326 of this process depends on the amount of phosphate stored. Hill function is proposed to
327 simulate the influence of internal phosphorus concentration on ammonium removal rate since
328 a sharp increase was observed when biomass P content exceeded 2.2%.
- 329 - Microalgal ammonium uptake rate depends on ammonium concentration. The Monod
330 kinetics is used to simulate this dependency.

331 - Biomass is assumed to have a constant composition, excluding the polyphosphate internally
332 stored, which is itself a separate component in the model.

333 -Phosphate uptake and thus intracellular phosphate accumulation is not considered in the
334 model since this process was not experimentally studied (took place only once when P was
335 supplemented) and thus experimental data is insufficient for obtaining the corresponding
336 kinetic constants. It is considered that the amount of phosphate removed from the medium
337 becomes intracellular polyphosphate. As previously explained, chemical precipitation is
338 avoided with pH control.

339 -Microalgal death is modelled using a first order kinetics: death rate depends on microalgal
340 concentration. Microalgal death produces inert particulate organic material, with the same N
341 and P composition as the active biomass. No solubilisation processes are considered. The
342 polyphosphate of the dead cells is considered to stay unavailable for further microalgal
343 growth.

344 -The light influence on the microalgal growth is modelled using the Steele function (1), as
345 suggested by [26] or [27]. A weighted average light intensity, which takes into account the
346 reactor's geometry and the self-shading factor of the microalgae, is used. It is calculated
347 dividing the reactor into discrete concentric sections and applying Lambert-Beer's Law (2) for
348 calculating a uniform light for each section.

349
$$\frac{I}{k_i} \exp\left(1 - \frac{I}{k_i}\right) \quad (1)$$

350
$$I = I_0 \cdot \exp(-a \cdot TSS \cdot z) \quad (2)$$

351 Where I is light intensity ($\mu\text{E}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$), k_i is the optimal light intensity ($\mu\text{E}\cdot\text{m}^{-2}\cdot\text{s}^{-1}$), a is the
 352 microalgal self-shading factor ($\text{m}^2\cdot\text{gTSS}^{-1}$), and z (m) is the distance from the surface of the
 353 reactor.

354 The components considered in the model are:

355 X_{Alg} , microalgal biomass, expressed in $\text{mgCOD}\cdot\text{l}^{-1}$, excluding internally accumulated
 356 polyphosphate.

357 X_{PP} , intracellular stored polyphosphate, expressed in $\text{mgP}\cdot\text{l}^{-1}$. It is not included in the mass of
 358 X_{Alg} .

359 X_{Deb} , inert particulate organic material, expressed in $\text{mgCOD}\cdot\text{l}^{-1}$. Generated in the death
 360 process of microalgae, this component accumulated in the reactor during the experiment.

361 S_{NH_4} , ammonium concentration in the medium, expressed in $\text{mg NH}_4\text{-N}\cdot\text{l}^{-1}$.

362 The kinetic equations proposed for microalgal growth (3) and death (4) are:

$$363 \quad r = \mu \cdot X_{Alg} \cdot \frac{S_{NH_4}}{K_S + S_{NH_4}} \cdot \frac{I}{k_i} \cdot \exp\left(1 - \frac{I}{k_i}\right) \cdot \left(1 - \frac{k_{XPP}^n}{k_{XPP}^n + \left(\frac{X_{PP}}{X_{Alg}}\right)^n}\right) \quad (3)$$

$$364 \quad r = b \cdot X_{Alg} \quad (4)$$

365 The time evolution of all the components can be obtained from the following differential
 366 equations:

$$367 \quad \frac{dX_{Alg}}{dt} = \mu \cdot X_{Alg} \cdot \frac{S_{NH_4}}{K_S + S_{NH_4}} \cdot \frac{I}{k_i} \cdot \exp\left(1 - \frac{I}{k_i}\right) \cdot \left(1 - \frac{k_{XPP}^n}{k_{XPP}^n + \left(\frac{X_{PP}}{X_{Alg}}\right)^n}\right) - b \cdot X_{Alg} \quad (5)$$

$$368 \quad \frac{dS_{NH_4}}{dt} = -i_{N_{Alg}} \cdot \mu \cdot X_{Alg} \cdot \frac{S_{NH_4}}{K_S + S_{NH_4}} \cdot \frac{I}{k_i} \cdot \exp\left(1 - \frac{I}{k_i}\right) \cdot \left(1 - \frac{k_{XPP}^n}{k_{XPP}^n + \left(\frac{X_{PP}}{X_{Alg}}\right)^n}\right) \quad (6)$$

$$369 \quad \frac{dX_{PP}}{dt} = -i_{P_{Alg}} \cdot \mu \cdot X_{Alg} \cdot \frac{S_{NH_4}}{K_S + S_{NH_4}} \cdot \frac{I}{k_i} \cdot \exp\left(1 - \frac{I}{k_i}\right) \cdot \left(1 - \frac{k_{XPP}^n}{k_{XPP}^n + \left(\frac{X_{PP}}{X_{Alg}}\right)^n}\right) - b \cdot X_{PP} \quad (7)$$

$$370 \quad \frac{dX_{Deb}}{dt} = b \cdot X_{Alg} \quad (8)$$

371 Where $i_{P_{Alg}}$ ($\text{gP} \cdot \text{gCOD}^{-1}$) is the phosphorus content of the microalgal structure (constitutional
372 P in X_{Alg}), $i_{N_{Alg}}$ ($\text{gN} \cdot \text{gCOD}^{-1}$) is the nitrogen content of the microalgal structure, μ is the
373 maximal growth rate (h^{-1}), K_S represents the halfsaturation constant for ammonium ($\text{mgN} \cdot \text{l}^{-1}$),
374 k_{XPP} represents the ratio X_{PP}/X_{Alg} that leads to a 50% reduction of the maximal growth rate
375 ($\text{gP} \cdot \text{gCOD}^{-1}$), n is a constant from Hill function, and b is the microalgae death rate (h^{-1}).

376 **3.2.2. Model calibration**

377 Model parameters were determined using the Solver program in Microsoft [®] Excel software
378 2007 for minimizing the residual sum of squared errors between the two sets of experimental
379 data (ammonium concentrations in *N&PR* and *NOR*) and the model predictions.

380 Initial microalgae, debris, and polyphosphate concentrations are required in order to solve the
381 differential equations. These values can be estimated from suspended COD and TSP
382 measurements (9 and 10) jointly with the steady-state debris balance (11) applied to the
383 reactor where the microalgae were cultivated in semicontinuous mode.

$$384 \quad \text{susp. COD} = X_{Deb} + X_{Alg} \quad (9)$$

$$385 \quad \text{TSP} = X_{PP} + i_{P_{XAlg}} \cdot X_{Alg} \quad (10)$$

$$386 \quad b \cdot X_{Alg} \cdot \theta = X_{Deb} \quad (11)$$

387 where θ is the cellular retention time in the semicontinuous reactor where the microalgae used
388 for inoculum were cultivated.

389 The corresponding boundary conditions were set in the solution procedure every time a
390 reactor was spiked with ammonium. Polyphosphate concentration in *N&PR* was increased
391 according to the observed phosphate decrease during the following 7 hours after the
392 phosphate addition. The initial values for the model parameters were selected based on
393 previous experience and on literature. All concentrations were calculated with a time step of 5
394 minutes.

395 i_{NAlg} was established at the initial nitrogen biomass composition (9% $\text{gN}\cdot\text{gCOD}^{-1}$) and for
396 i_{PAlg} a value of 0.1% ($\text{gP}\cdot\text{gCOD}^{-1}$) was chosen, which is necessarily below the phosphorus
397 total composition of 0.5% ($\text{gP}\cdot\text{gCOD}^{-1}$) at the end of the experiment and accounts only for
398 structural phosphorus and not polyphosphate. Figs. 3a and 3b show the model predictions for
399 ammonium concentration and the experimental values along the experiment for *NOR* and
400 *N&PR*, respectively. The obtained parameters, shown in table 3, accurately reproduce the
401 experimental data in both reactors, as shown in fig. 4, where predicted values are plotted
402 against their analytical values with a Pearson correlation coefficient of $r = 0.952$ (P-value <
403 0.01, statistical analysis carried out using SPSS 16.1).

404 For further model validation, a set of data from a shorter but analogous experiment was used.
405 The experiment consisted of an identical reactor where the same procedure as in *N&PR* was
406 followed, with the difference that phosphate was added to the medium after 7 days and the
407 experiment was stopped after 18 days. Moreover, phosphorus was added at a higher
408 concentration of $37 \text{ mgP}\cdot\text{l}^{-1}$ (fig. 5). Biomass, ammonium and phosphate were characterized
409 as described in section 2.4 in this work. The parameters shown in table 3 were introduced in

410 the model to obtain the corresponding predicted values, which are shown in fig. 5, and also
411 plotted versus their analytical values in fig. 4. The obtained accuracy ($r = 0.97$, P-value <
412 0.01) confirms the suitability of the model and the determined parameters.

413 One of the most important effects of the higher concentration of added phosphate was that
414 X_{PP}/X_{Alg} ratio reached a maximum of 4% $\text{mgP} \cdot \text{mgTSS}^{-1}$. The simulation shows that from day
415 12 of the experiment biomass P content stayed stable around 3% $\text{mgP} \cdot \text{mgTSS}^{-1}$, since
416 ammonium was not available for growth. The high internal phosphorus concentration
417 achieved might be the reason why remaining phosphate in the medium was not taken up by
418 the microalgae during this period, as can be seen in fig. 5.

419 The values obtained for μ and k_S are comparable to those obtained by [24]. These authors fit
420 ammonium uptake by *Scenedesmus* sp.LX1 using a Monod equation and obtained values
421 between 0.005 - 0.025 h^{-1} for μ and 4.5 - 13.3 $\text{mgN} \cdot \text{l}^{-1}$ for K_S . The obtained value for k_{XPP} is in
422 complete accordance with the observations made. Literature k_i values vary in a wide range
423 between 20 and 500 $\text{W} \cdot \text{m}^{-2}$ ([28] and [26], respectively), in which our 200 $\mu\text{mol} \cdot \text{m}^2 \cdot \text{s}^{-1}$ would
424 be included. The selfshading factor, a , also varies in a wide range in literature. Similar values
425 to ours are used in [29-30]. The value obtained in this study for microalgae death rate ($b =$
426 0.002 h^{-1}) compares with literature values ranging from 0.0008 h^{-1} [31] to 0.0058 h^{-1} [32].

427 Measured and predicted COD values are shown in table 4, together with predicted X_{Alg} and
428 X_{Deb} . The predictions of the COD values for initial reactor are in very good accordance with
429 measured values. For *NOR* and *N&PR* the model underestimates COD. Because of the higher
430 mean analytical error in COD measurements, the model has been calibrated to minimize the
431 error in the response for ammonium concentration. The parameters obtained are those which
432 allow the best prediction of ammonium concentration and not of suspended COD values. On

433 the other hand, the assumption of a constant microalgal N composition (set to its initial
434 measured value of 9%) is a simplification of reality. With a different and/or varying
435 microalgal N content, predicted COD values would have been certainly different. Including a
436 variable microalgae N content according to factors such as N stress, etc., might be the way for
437 improving a model of this kind. This was, however, out of the scope of this paper.

438 **4. CONCLUSIONS**

439 Microalgal growth and ammonium removal in the absence of phosphorus were studied in two
440 mixed cultures of autochthonous microalgae. The results showed that microalgal growth and
441 phosphorus uptake are independent processes. It was also proved that ammonium removal
442 rate depends on the amount of phosphorus internally stored. The proposed microalgal growth
443 model, which includes a Monod term for the effect of ammonium concentration, Hill's
444 function for the effect of the stored polyphosphate concentration and Steele's function for
445 light influence, accurately reproduced the experimental data. Further research should make
446 use of these results for the development of nutrient removal strategies using microalgal
447 cultures.

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548 **FIGURE LEGENDS**

549 Fig. 1: a) Experimental setup; b) illumination and measuring point.

550 Fig. 2: Ammonium and phosphate evolution in a) *NOR* and b) *N&PR* during the whole
551 experiment.

552 Fig. 3: Time evolution of ammonium concentration in a) *NOR* and b) *N&PR*, along with
553 model predictions.

554 Fig. 4: Predicted values plotted against their corresponding analytical values. Empty dots
555 correspond to this experiment for model calibration and full dots correspond to data from
556 previous experiment for model validation.

557 Fig. 5: Time evolution of ammonium and phosphate concentrations in the model validation
558 dataset, along with model predictions.

559

560 TABLES

561

562 Table 1: Biomass evolution in the reactors and calculated yields.

Time (d)	TSS ^a (mg·l ⁻¹)	VSS ^a (mg·l ⁻¹)	Susp COD ^b (mg·l ⁻¹)	Biomass N content (gN·gVSS ⁻¹)	Biomass P content (gP·gVSS ⁻¹)	Yield coefficient Y _{N-VSS} (gVSS·gN ⁻¹)	Yield coefficient Y _{N-COD} (gCOD·gN ⁻¹)
0	380	340	517	11.8%	3.7%	--	--
19 (end of <i>initial reactor</i>)	882	817	1176	12.0%	1.6%	8.2	11.3
46 (end of <i>NOR</i>)	1330	1224	1880	10.8%	0.8%	8.8	12.8
46 (end of <i>N&PR</i>)	1583	1460	2320	10.6%	1.7%	8.7	13.9

563 Mean analytical error: ^a 50 mg·l⁻¹; ^b 70 mg·l⁻¹;

564

565

566 Table 2: Calculated net and specific ammonium removal rate after each ammonium addition
 567 in each reactor, together with biomass P content at those moments (beginning of slope).

Reactor	Slope number	Removal rate (mgN·l ⁻¹ ·h ⁻¹)	Slope error	Specific removal rate (mgN·mgVSS ⁻¹ ·h ⁻¹)	Biomass P content (gP·gVSS ⁻¹)
<i>initial</i>	1	0.209	0.018	6.15x10 ⁻⁴	3.7%
	2	0.121	0.002	2.11x10 ⁻⁴	2.2%
<i>N</i>	3	0.152	0.001	1.86x10 ⁻⁴	1.6%
	4	0.090	0.009	8.79x10 ⁻⁵	1.0%
<i>P</i>	3	0.514	0.051	6.07x10 ⁻⁴	2.6%
	4	0.247	0.004	2.41x10 ⁻⁴	2.0%
	5	0.176	0.014	1.41x10 ⁻⁴	1.5%

568

569

570 Table 3: Obtained parameters

Parameter	Units	Obtained value
μ	h^{-1}	0.042
k_S	$\text{mgN}\cdot\text{l}^{-1}$	12
n	-	1.35
K_{XPP}	$\text{mgP}\cdot\text{mgCOD}^{-1}$	0.027
k_I	$\mu\text{E}\cdot\text{m}^2\cdot\text{s}^{-1}$	200
b	h^{-1}	0.0005
a	$\text{m}^2\cdot\text{gTSS}^{-1}$	0.03

571

572

573 Table 4: Measured COD values. Predicted total COD, X_{Alg} and X_{Deb} values.

Time (d)	Measured Susp COD ($\text{mg}\cdot\text{l}^{-1}$)	Predicted Susp COD ($\text{mg}\cdot\text{l}^{-1}$)	X_{Alg} ($\text{gCOD}\cdot\text{l}^{-1}$)	X_{Deb} ($\text{gCOD}\cdot\text{l}^{-1}$)
0 (inoculum)	517	517	434	83
19 (end of <i>initial reactor</i>)	1176	1132	535	596
46 (end of <i>NOR</i>)	1880	1554	357	1196
46 (end of <i>N&PR</i>)	2320	1624	412	1212

574

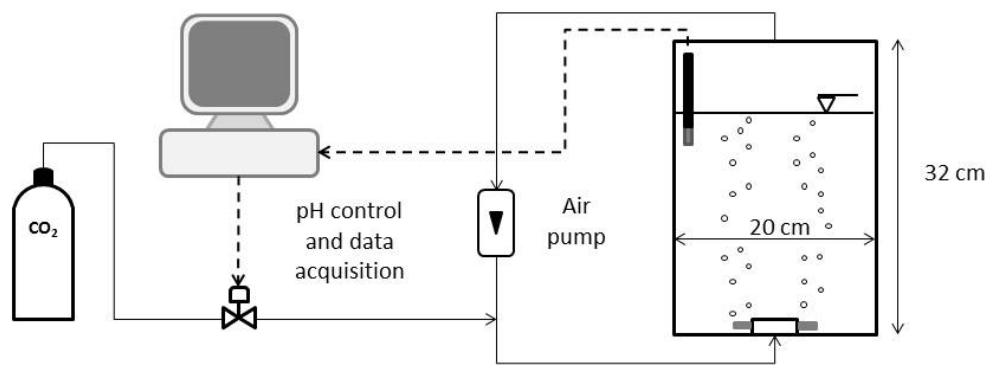
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576 FIGURES

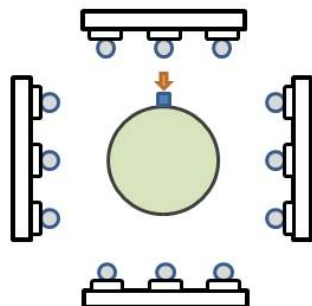
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578 Fig. 1

579



a)



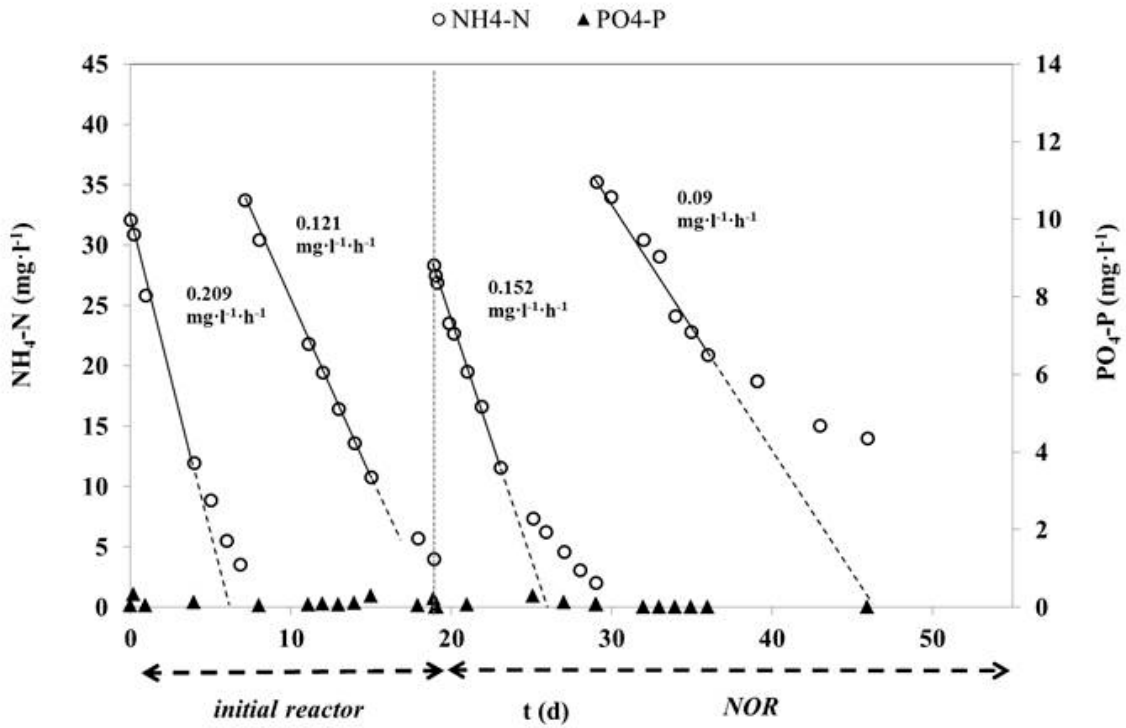
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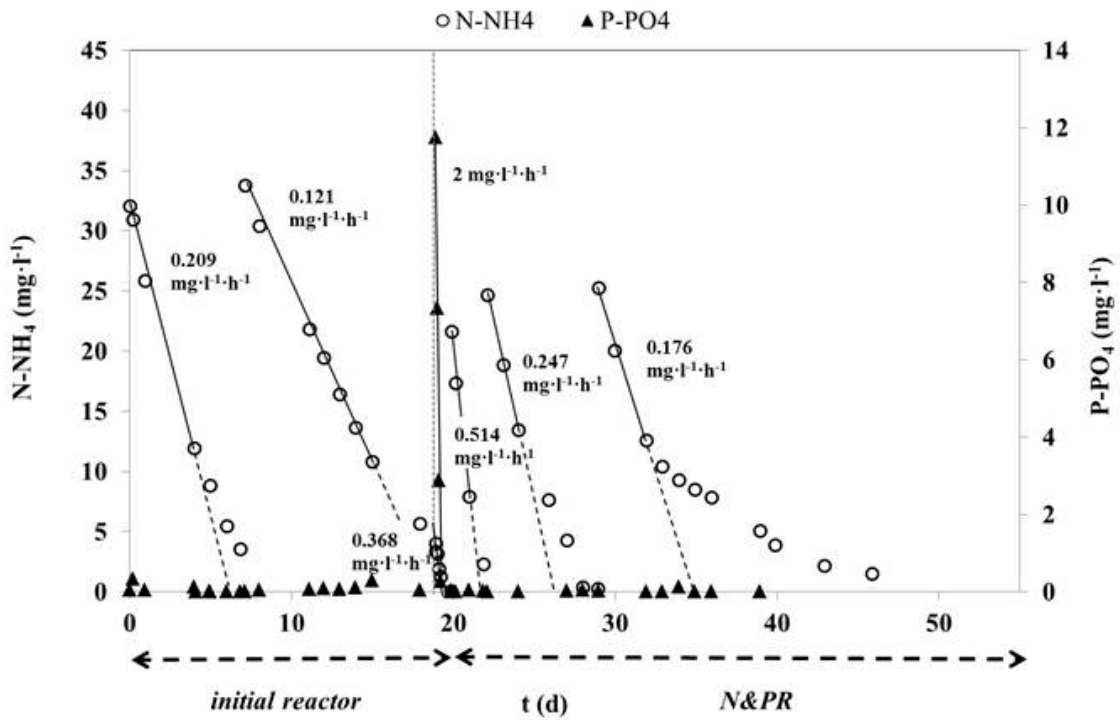
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582 Fig. 2

583



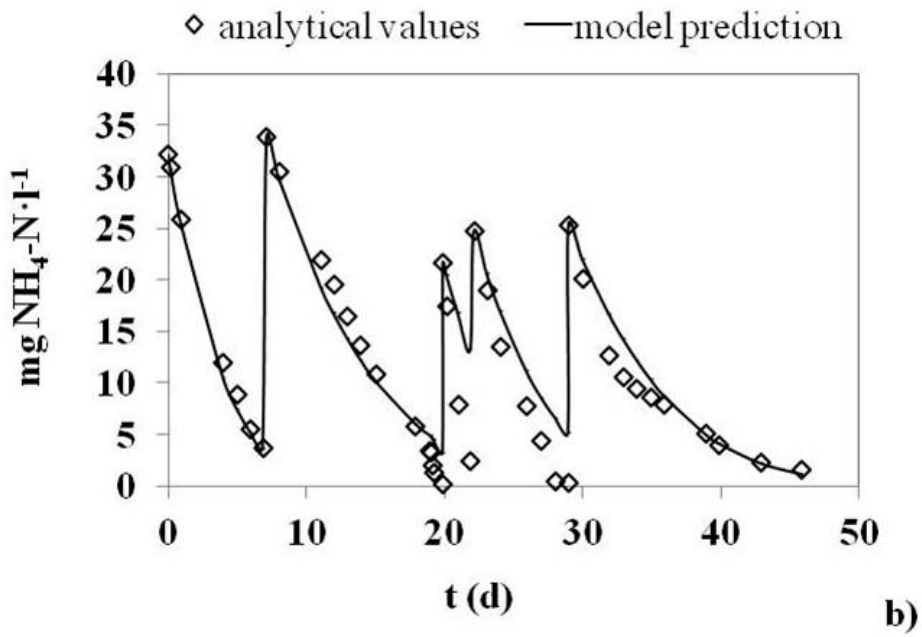
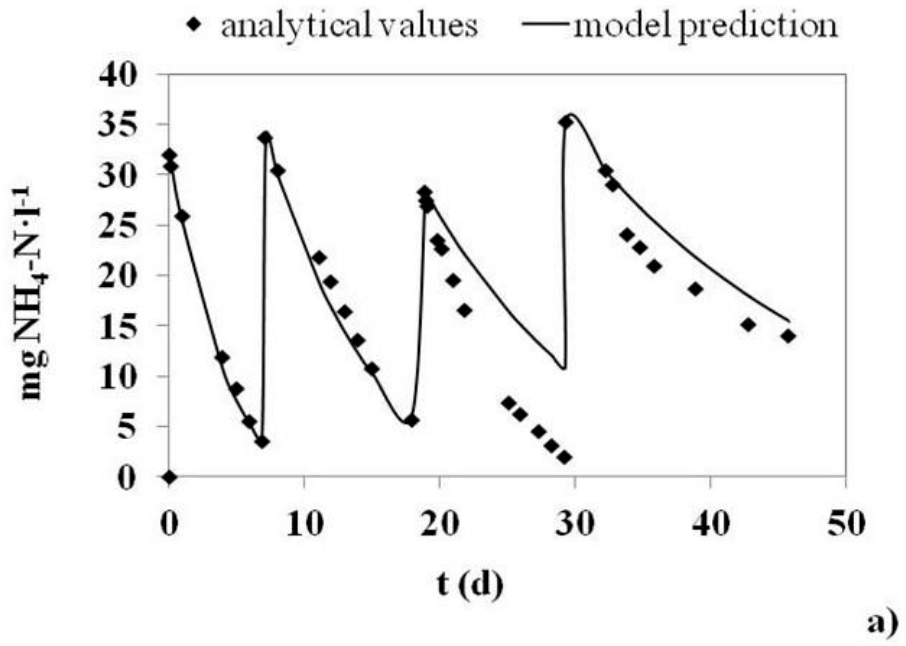
a)



b)

584

585 Fig. 3



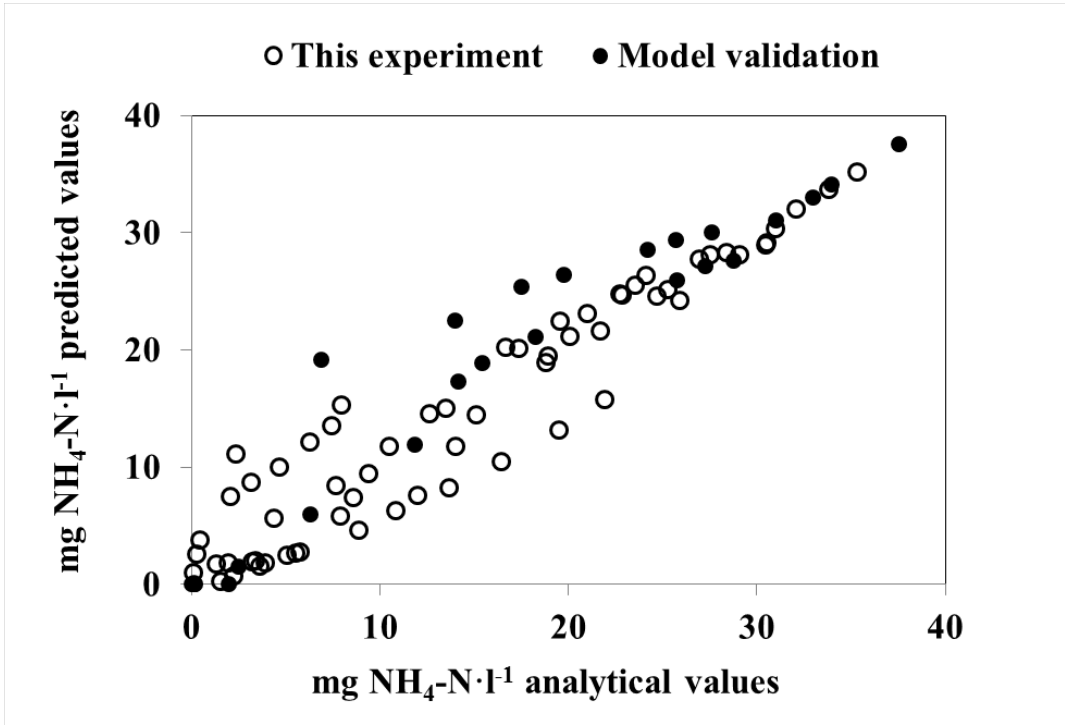
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589 **Fig. 4**

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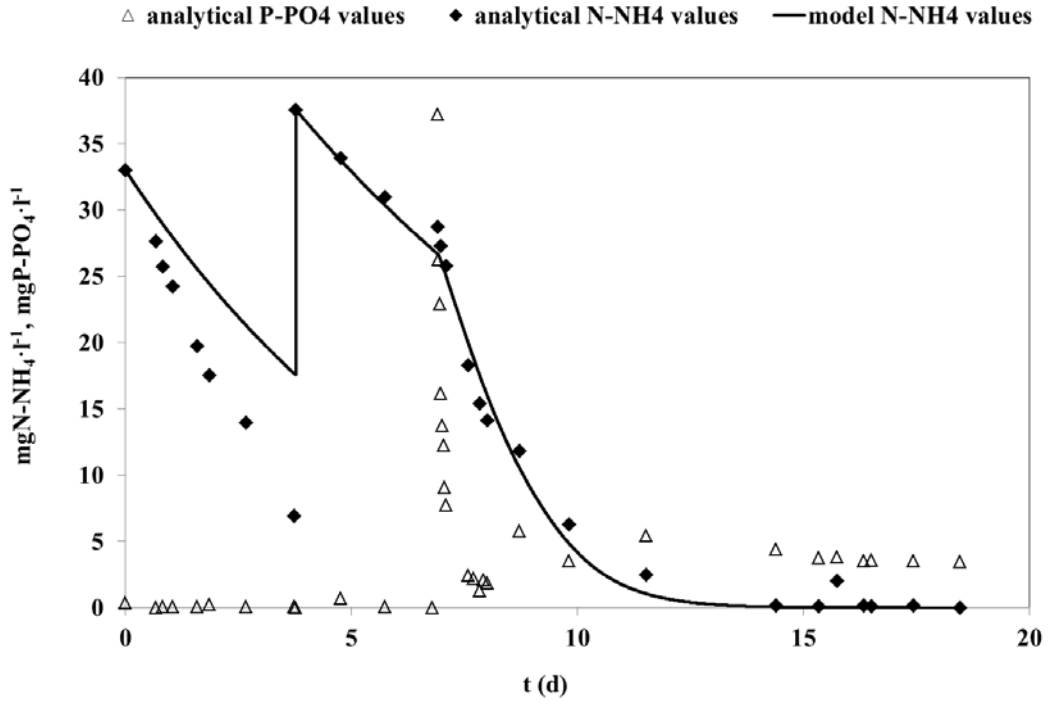


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593 Fig. 5

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595